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Editorial Preface

From the Desk of Managing Editor...

Artificial Intelligence is hardly a new idea. Human likenesses, with the ability to act as human, dates back to Geek mythology with Pygmalion's ivory statue or the bronze robot of Hephaestus. However, with innovations in the technological world, AI is undergoing a renaissance that is giving way to new channels of creativity.

The study and pursuit of creating artificial intelligence is more than designing a system that can beat grand masters at chess or win endless rounds of Jeopardy!. Instead, the journey of discovery has more real-life applications than could be expected. While it may seem like it is out of a science fiction novel, work in the field of AI can be used to perfect face recognition software or be used to design a fully functioning neural network.

At the International Journal of Advanced Research in Artificial Intelligence, we strive to disseminate proposals for new ways of looking at problems related to AI. This includes being able to provide demonstrations of effectiveness in this field. We also look for papers that have real-life applications complete with descriptions of scenarios, solutions, and in-depth evaluations of the techniques being utilized.

Our mission is to be one of the most respected publications in the field and engage in the ubiquitous spread of knowledge with effectiveness to a wide audience. It is why all of articles are open access and available view at any time.

IJARAI strives to include articles of both research and innovative applications of AI from all over the world. It is our goal to bring together researchers, professors, and students to share ideas, problems, and solution relating to artificial intelligence and application with its convergence strategies. We would like to express our gratitude to all authors, whose research results have been published in our journal, as well as our referees for their in-depth evaluations.

We hope that this journal will inspire and educate. For those who may be enticed to submit papers, thank you for sharing your wisdom.

Editor-in-Chief

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Mobile Subscription, Penetration and Coverage Trends in Kenya's Telecommunication Sector

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Abstract—Communication is the activity of conveying information through the exchange of thoughts, messages, or information, as by speech, visuals, signals, writing, or behavior. In Kenya the mobile subscription, penetration and coverage have been growing since the first mobile operators started operating in 1999. The current mobile operators in Kenya are given by Safaricom Ltd, Airtel Networks Kenya Ltd, Essar Telecom Kenya Ltd and Telkom Kenya Ltd (TKL-Orange).

This paper discusses the present condition of the telecommunication sector in Kenya and the trends in subscription, penetration and coverage since 1999 when the first two mobile operators (Safaricom Ltd and Celtel now as Airtel Networks Kenya Ltd) started their operations and later the introduction of two other operators Essar Telecom Kenya Ltd and Telkom Kenya Ltd (Orange brand) in 2008. The paper also tries to find out what is likely to happen in a few years to come and provision of a set of recommendations based on the analysis. The study was based on extensive literature review and secondary data sources mainly from Communication Authority of Kenya (CAK). The data obtained was analyzed using Matlab and Microsoft excel to obtain the relevant graphical representations as given in results and discussions.

Keywords—Communication; Telecommunication; Cellular phone; Civilization; Trends

I. INTRODUCTION

Communication has been part and parcel of the human race since time immemorial. Telecommunication is the science of transferring information over long distances by electrical and electromagnetic waves which started with the telegraph, telephone, radio, television, satellites, internet and now commonly mobile communication. It can also be said to represent any process or group of processes that allow the transmission of audio, video information or data over long distance by means of electromagnetic or electrical signals. The invention of a practical telegraph in the late 1830s and the telephone in 1876 brought humanity into the era of electrical telecommunications. After over 100 years of triumph, public telegraphy left the communications market. But telex took over and evolved into massively popular forms such as SMS and email, while telephony remains the most widely used means of communication in the world today. Over the past century or so, communications technologies have advanced from manual to automatic switching and from analog to digital

communications, alongside many other major technological revolutions.

However, the greatest changes in consumer experience did not occur until mobile phone and the Internet came out and became common elements of life, and which continue to generate even larger changes [1].

In our study we shall look at it as the transfer of information from one location to the other using mobile phone or cellular phone.

In earlier times a "Telephone" was a symbol of status. It was quite a difficult and lengthy process for one to have a telephone connection at his/her home. This time provided by only telecom Kenya up to 1999 when we had the entrance of mobile operators Safaricom and Celtel. In case of an emergency when someone needed to call abroad there was so much harassment in getting a line or if you were lucky to get it, was not clear, distance call rate was so high that sometimes poor people could not afford. Even locally for those who were not lucky enough to get a line had to make long queues behind a telephone booth (located at long distances from one's home) to make a call. But now the situation is totally changed in that technology is available which can avail the information within a very short time thanks to mobile phones. This has drastically changed our lives by making it easy for us as everyone can attest to this. Employment opportunities have increased whereby most graduates get placed in formal employment in the telecommunication sector which can take graduates from various fields.

For instance telecommunication, information technology, human resource and other graduates can easily fit into this sector. The Government has also greatly benefited from the revenues from this sector taking an example of companies like Safaricom contributing up to a tune of several billions in a year. Also information technology has got a big boost by mobile phone technology growth more so in the mobile application software development section. These rapid changes have been made possible with the mobile technology growth. From the information found in the yearly reports from Communications Authority of Kenya (CAK) reveals that mobile phone subscription in Kenya reached the 32.2 million subscriptions by June 2014 [2]. The mobile penetration has not been left behind in which case it has also been increasing from 1999 to march 2014 where it hit a high of 78%.

A. Statement of the problem

Information communication technology is an important sector in any country where it plays a very important role in a nation's economy. Researchers have not looked into the study of the trends of mobile subscription and penetration over the period from 1999 to 2013. This research is intended to have a detailed study on the trends of this industry in Kenya and maybe world over. This can help the telecommunication industry understand the trends and what is likely to happen in the near future so that they can give it a strategic response.

The telecommunications industry in Kenya has been undergoing rapid changes. The Communications Authority of Kenya has in the past 15 years licensed four mobile operators (Safaricom, Airtel and Essar (Yu); all of which are global operators) and several internet service providers like Wananchi and Jamii Telkom. Clearly, competition in this sector has greatly intensified in both the voice and data service provision.

B. Research objectives

The broad objective of the paper is to make an extensive study on the trends experienced in the telecommunication sector in Kenya. The specific objectives are:

- Determine the mobile subscription trend in Kenya.
- Determine the mobile penetration trend in Kenya.
- Analyze the above two.
- To find out the determinants that affects the expansion (growth) of the sector.

C. Importance of the study

The study would be valuable to several stakeholders for the following reasons:

- 1) Enable the telecommunication companies to know the trends in mobile subscription in Kenya.
- 2) Help companies to make informed future plans.
- 3) Enable the telecommunication companies to know the trends in mobile penetration in Kenya.
- 4) Telecommunication companies can use the findings to develop appropriate policies and strategic responses to the challenges as result of the rate of subscription and penetration.
- 5) Enable CAK to give proper guidance to the mobile phone operators.

The study would also provide a source of inspiration to a researcher for self-professional development and enrichment.

II. LITERATURE REVIEW

A. Telecommunication sector in Kenya

Up to date there are four mobile operators in our country namely Safaricom Ltd, Airtel Networks Kenya Ltd, Essar Telecom Kenya Ltd and Telkom Kenya Ltd (Orange). According to the mobile subscription and profitability Safaricom Ltd is in the top position among the four operators [2]. The other companies have lower market shares as shown in the study but their main companies are the world's famous

and big organizations like Airtel has very high subscription in most Asian countries including India (highest with 183.61 million subscribers as of November 2012) and Bangladesh (third with 5.1 million subscribers as of June 2011) [3]. They have invested a lot and also have more plans for investment having in mind that their key objective is to earn profits. By the end of the third quarter of the 2013/14 financial year (June, 14), there were a total of 32.2 million subscriptions in the mobile telephony market segment up from 31.8 million posted in the previous quarter. This represents an increase of 5.6 percent during the period. Mobile penetration grew to reach 79 percent from 78 recorded at the close of the previous quarter.

B. Mobile subscription

Mobile cellular telephone subscriptions are subscriptions to a public mobile telephone service using cellular technology, which provide access to the public switched telephone network. Post-paid and prepaid subscriptions are included [4]. The number of mobile subscribers usually gives an indication of how vibrant the telecommunication sector of a country is. It also shows the rate of growth of the sector. It can help many companies determine their stage of growth and respond strategically to the different challenges that come with each stage. The market share for each player in this field can also be determined using this very important indicator.

C. Mobile penetration

Mobile phone penetration rate is a term generally used to describe the number of active mobile phone numbers (usually as a percentage) within a specific population [5]. This value can go beyond 100% due the fact that one person can have more than one SIM-card. This can be noted from countries like Qatar which has 170% [6] and most of Europe with 128% [7].

D. Mobile coverage

In telecommunications, the coverage of a radio station is the geographic area where the station can communicate. Broadcasters and telecommunications companies frequently produce coverage maps to indicate to users the station's intended service area. Coverage depends on several factors, such as orography (i.e. mountains) and buildings, technology, radio frequency, transmitted power and distance from the station. Some frequencies provide better regional coverage, while other frequencies penetrate better through obstacles, such as buildings in cities.

The ability of a mobile phone to connect to a base station depends on the strength of the signal. That may be boosted by higher power transmissions, better antennae and taller antenna masts. Signals will also need to be boosted to pass through buildings, which is a particular problem designing networks for large metropolitan areas with modern skyscrapers. Signals also do not travel deep underground, so specialized transmission solutions are used to deliver mobile phone coverage into areas such as underground parking garages and subway trains. This is the same case with indoor coverage [8]. This is also an important parameter in showing the number of people who are likely to receive a signal depending on their location. This parameter can go up to a maximum of 100% since it deals with the area occupied by a country.

III. RESEARCH METHODOLOGY

A. Research design and data collection

This study basically covers a period of 13 years starting from 1999 to 2013. An attempt has also been made to include the latest information whenever available.

Much of the information for this research was obtained from secondary sources i.e. the internet e-journals, e-books and websites. This was done by collecting data from the reports of the Communications Commission of Kenya (CAK), via the internet.

Annual reports of different telecom companies, articles published in newspapers, conference papers and seminars proceedings were also carefully studied to procure the needed information. The report only presents simple frequency and quantitative tables. Various statistical tools and techniques have been applied for the analysis and interpretation of data.

B. Data analysis

For this study, the content analysis technique was employed to analyze the data. Matlab and Microsoft Excel Spread Sheet, with the associated trend analysis and graphical representation techniques were used to analyze quantitative data. The full report on the key findings of this study by the researcher is presented in section below.

IV. FINDINGS AND DISCUSSIONS

A. Introduction

This section deals with analysis and discussion of the research findings. Data was collected from the CAK website in which case the mobile subscription and penetration are analyzed. Following is a report on the key findings of this study by the researcher.

B. Market share analysis of telecom sector in Kenya:

TABLE I. TOTAL MOBILE SUBSCRIPTIONS

Subscription Type	June-14	March-14	Quarterly Variation (%)
Prepaid Subscriptions	31,580,696	31,222,434	1.1
Post-Paid Subscriptions	665,697	607,569	9.5
Total Mobile Subscriptions	32,246,393	31,830,003	1.3

Mobile subscription by June 2014

By June 2014 the total number of mobile subscriptions was recorded as 32.2 million up from 31.8 million posted in the previous quarter (March the same year). This represents an increase of 5.6 percent during the period. The continued growth in mobile subscriptions indicates that there is still opportunity for growth in the mobile telephony services. However, the rate of growth in the subscriber base is flattening as the sector progressively tends towards maturity. Consistent, attractive promotions and special offers coupled with competitive retail tariffs could have contributed to the increase in subscriptions during this period. The prepaid subscriptions

grew by 1.1 percent during the period compared to 9.5 percent growth recorded in post-paid subscriptions. Even though the growth rate for post-paid subscriptions was more than that for pre-paid, the ratio of prepaid subscriptions continued to dominate and represented 98.0 percent of the total mobile subscriptions. This is consistent with the trends in developing countries where prepaid service is preferred due to the ease and convenience of subscription compared to postpaid which has requirements that are not within the reach of the majority of the population. The reduction of the value of prepaid calling cards to as low as KES 5.00 has made prepaid services a choice for most low income subscribers. Besides the availability of low value cards one can now easily access credit through money transfer methods like M-pesa and advance credit like Okoa Jahazi.

The growth of mobile subscriptions is shown in Table I.

Among the operators at the end of June 2014, Safaricom had the highest subscriber with 21,928,450, Airtel is in the second positions with the total subscriber base of 5,068,765, Essar Telecom Kenya Limited with 2,563,810 and then Telkom Kenya Limited (Orange) with 2,685,368 subscribers which stands as the fourth largest mobile phone operator in Kenya.

During the period under review, three mobile operators recorded positive gains in subscriptions. Telkom Kenya Limited (Orange) recorded the highest gains in new subscriptions of 231,470, representing a growth of 9.4 percent compared to the previous quarter. Safaricom Limited gained 361,062 (1.7% growth) new subscribers while Airtel Networks

Kenya Limited lost 130,005 (-3.5 % growth). Essar Telecom Kenya Limited on the other hand gained 511,526 subscriptions, representing 0.2 percent increase from the previous quarter. The following table shows the number of mobile subscribers in Kenya as of June 2014 [2].

TABLE II. MOBILE SUBSCRIPTIONS PER OPERATOR

Name of operator	June-14		
	Pre-paid	Post-paid	Total
Safaricom Limited	21,405,667	522,783	21,928,450
Airtel Networks Kenya Limited	4,930,774	137,991	5,068,765
Essar Telecom Kenya Limited	2,562,339	1,471	2,563,810
Telkom Kenya Limited (Orange)	2,681,916	3,452	2,685,368
Total	31,580,696	665,697	32,246,393

March-14			Quarterly Variation (%)
Pre-paid	Post-Paid	Total	
21,094,414	472,974	21,567,388	1.7
5,121,082	130,005	5,251,087	-3.5
2,556,110	1,520	2,557,630	0.2
2,450,828	3,070	2,453,898	9.4
31,222,434	607,569	31,830,003	1.3

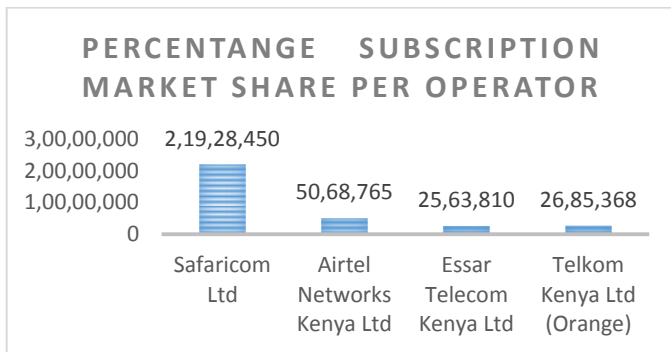


Fig. 1. Percentage market share per operator as of June 2014

The level of market share measured by subscription is still dominated by Safaricom. Safaricom Ltd market share by subscription was 68 percent during the period under review. Telkom’s (Orange) market share percentage points stands at 8 percent at the end of the quarter.

Airtel Networks Kenya Limited’s market share is given by 16 percent while that of Essar Telecom’s is at 8 percent. The market share by subscription by operator is shown in Figure 1.

Mobile subscription from 1999 to 2013

The table below summarizes the key findings on the mobile subscription from the year 1999 to 2013. The data provided is on yearly basis taking subscription as of December each year.

Since the Communication Authority of Kenya (CAK) then CCK issued the two mobile licenses in 2000 (Safaricom and Celtel now Airtel), the mobile telecommunication continued to be popular with consumers. For the first five years the sub sector registered over 60% annual growth with over 16,233,833 subscribers at the end of December 2008. In 2005 the growth rate shot up to 106% but then started declining from 2006 to December 2011 where it was 12%. The sudden increase could be attributed by the fact that around this time there were so many promotions. The difference between the subscribers in 2008 and 2007 was close to 4million because of the introduction of the other two mobile operators TKL-Orange brand and Essar Telkom Kenya limited in 2008.

TABLE III. MOBILE SUBSCRIPTIONS, 1999 TO 2013

Year	1999	2000	2001	2002
Number of mobile subscribers	15,000	114,000	585,131	1,325,222
2003	2004	2005	2006	2007
1,590,785	2,546,157	5,263,676	7,340,317	11,440,077
2008	2009	2010	2011	2012
16,233,833	19,364,559	24,968,891	28,080,771	30,731,754
2013				
31,830,003				

The highest difference was between 2010 and 2009 attributed most probably by the fact that the Orange grew with a higher rate and also the competition of the new entrants with the already existing mobile operators. From 2012 to 2013 increase was only 3.6 percent mostly as a result of sim card registration in Kenya where deadline was 2013 December.

Another reason is due to Mobile tariffs reducing significantly over the period registering an average of KES 2.65 for on-net calls per minute from KES 4.78 per minute in the previous period and KES 2.5 for post-paid subscribers at the end of the period under review.

This represents 33.4 per cent reduction on pre-paid tariffs and 55.5 per cent on post-paid tariffs from the previous period.

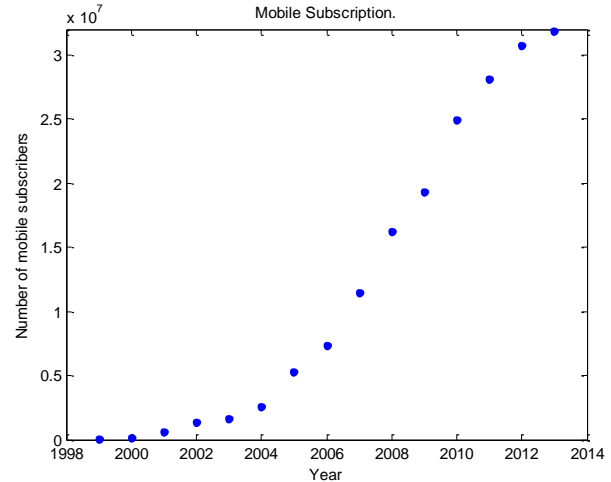


Fig. 2. Mobile subscription from 1999 to 2013

The tariff decline is attributed to an interconnection determination by the Commission during the period that saw mobile termination rates reduced to KES 2.21 from KES 4.42 coupled with increased competition among operators in the mobile market which followed the acquisition of Zain by Bharti Airtel whose business strategy seemed to target the mass market. The figure below is a graphical representation of the number of subscribers against the years.

TABLE IV. MOBILE SUBSCRIPTIONS GROWTH RATE

Year	1999	2000	2001	2002	2003	2004	2005
Mobile Subscriptions growth rate		660%	413%	126%	20%	60%	106%
2006	2007	2008	2009	2010	2011	2012	2013
39%	56%	42%	19%	29%	12%	8%	4%

Source: Research findings

From the graph we can be able to see that at the initial stages the growth was not as high as the later stages. Between 2004 and 2011 the growth rate was very high this is due to still there were several people in the country without mobile phone considering the total population of about 40 million. From 2011 onwards the subscription seems to start leveling. The leveling could be due to expected market maturity. Because of this mobile operators should introduce value added services to stay afloat. The services include additions to money transfer and different other mobile technologies (m-technologies). We can conclude that the graphical changes seem to follow a natural trend of exponential growth.

This is because at the initial stages there is a slow growth, the middle is characterized by high growth with steep gradient and towards the end the growth starts to flatten.

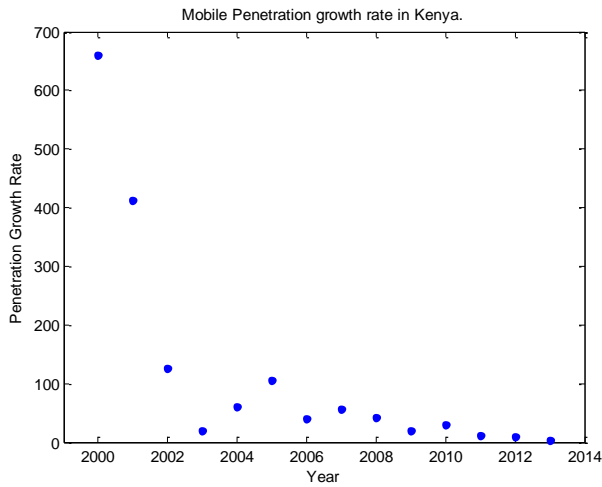


Fig. 3. Mobile subscriptions yearly growth rate

The figure above is a graphical representation of the penetration growth rate against the years. The graph shows that the period between 1999 and 2002 was high but decreasing by the year. This could be attributed by the fact that during this period the business was at its initial stages of growth. From 2003 to 2005 the growth rate increased. From 2005 to 2012 there were slight variations probably due market maturity in which most of the new subscribers are the youth.

Mobile penetration

Over the last thirteen years mobile penetration has registered an exponential growth from 0.053 in 1999 to 80 in December 2013. The increase in mobile penetration can be attributed to a number of factors. First, the reduction in the value of calling cards from the lowest of Kshs 250 in 1999 to Kshs 5 by September 2012 which has made calling cards affordable to low income earners thus stimulating this positive trend. Secondly, the average costs of making calls has declined from Kshs 27 to Kshs 1 to the same network. This has led to increased uptake of mobile phones as costs of calls become affordable thus increasing subscription rates and penetration. International call charges, on the other hand, have also changed over the period because of the use of VOIP technology. Third, even as the mobile operators adjust their tariffs, the mobile coverage has also increased with services now available to a higher population. The increase in mobile penetration can also be attributed to increase in the number of mobile operators from two in 1999 to four in 2008, increased mobile coverage.

The table above shows the mobile penetration in % in Kenya from 1999 to 2013. The mobile penetration per operator as of December 2013[2]

TABLE V. MOBILE PENETRATION

Year	1999	2000	2001	2002	2003	2004	2005
Mobile penetration %	0.053	0.38	1.90	4.20	4.95	7.77	15.74
2006	2007	2008	2009	2010	2011	2012	2013
21.62	33.65	43.64	49.7	63.2	71.3	78	79

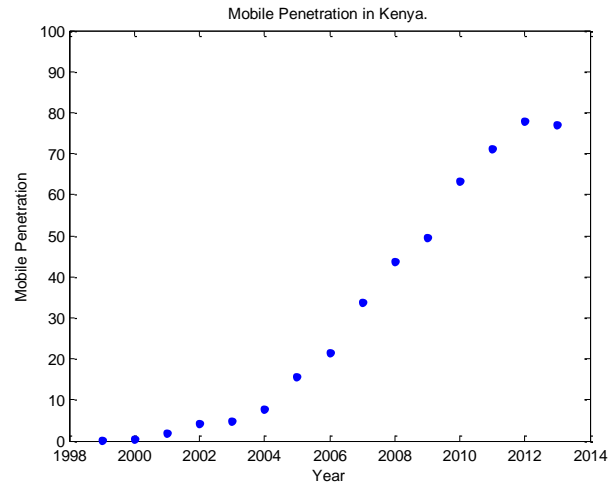


Fig. 4. Mobile penetration in Kenya

The graphical representation above is for mobile penetration against the years from 1999 to 2013. It can be noted that the rate is very low at initial stages being the time when the first two mobile operators were licensed in Kenya. This trend continued up to 2004 when the rate started growing. The growth saw high mobile penetration rate from this time to 2013. This could be attributed by the fact that there were high levels of competition between the first two operators which was even higher after the entrance of two other new operators Orange and Essar. In 2013 it declined probably because of the government policy that required that all mobile phone users and their sim cards be registered by December 2013 where the unregistered cases were to be locked out.

Mobile coverage

The current level of competition in the country has witnessed a network expansion by the four operators to levels that have surpassed their license conditions. This could be attributed to entry of the two mobile operators within the period of December 2008 which may have compelled the existing operators to expand their network coverage in order to solidify their market positions.

Establishment of new sites in areas hitherto considered uneconomical, has in effect increased the level of population coverage including some rural areas.

However, as is the case in most developing countries, this coverage is concentrated in areas with high population densities and promising economic potential especially in urban areas and along major highways. With a national coverage of about 77% of the population, the mobile industry invariably covers over 31 million people in the country. However, the 38% geographic coverage implies that many parts of the country are not covered especially the arid and semi-arid areas. The challenge is how to make these services affordable to the wider population and to encourage investment in high cost areas.

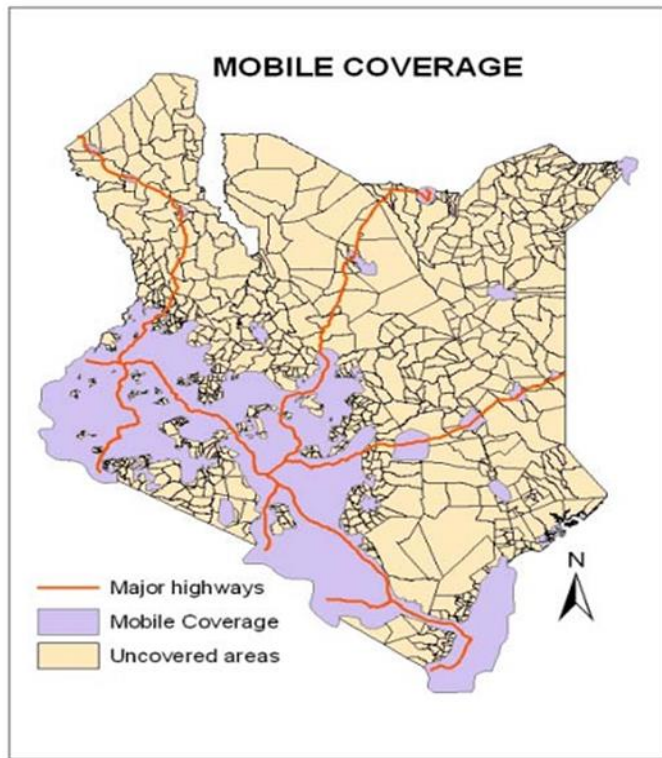


Fig. 5. A map of mobile coverage

As shown in the figure above the covered areas count for a mere 38% by June 2012 while the rest of the country remains uncovered.

V. SUMMARY, CONCLUSIONS AND RECOMMENDATIONS

A. Summary

The objectives of this study were to analyze the mobile subscription and penetration trends in the telecommunication industry in Kenya. The researcher found out that subscription and penetration rate have been growing since the first two companies Safaricom and Celtel (now Airtel) were licensed. By June 2014 the total number of mobile subscriptions was recorded as 32.2 million up from 15 thousand posted in 1999. Both mobile penetration and coverage have also been steadily growing.

B. Conclusion

There has been significant growth in telecommunication sector particularly in the use of mobile telephony. Competition among the operators, unification of the licenses and the

application of new technologies in mobile market segment has witnessed diversification of services by the operators, reduced tariff rates and increased affordability of communication services by a large population. This is further seen as a movement towards closing the digital divide.

The telecommunication landscape in Kenya has continued to be shaped by technological developments arising out of convergence and the new market structure. The subsequent shifts in consumer needs and expectations has compelled aggressive network roll out and infrastructure upgrades using technologies that support high capacity services. Increased competition among the operators has also contributed to the high level of product and service innovations as a means of customer acquisition and customer retention. This is as witnessed in the increase in subscriber base by the fixed network operator.

The outlook of the communication sector in Kenya continues to be strong, and growth will be achieved through gaining new customers, offering new services, and in general capitalizing on the growing role of telecommunications in people's everyday lives. The mobile sector in the country continues to grow increasingly competitive. This is shown with the steady growth in subscriptions.

Increased competition in the mobile sector has resulted in steady growth of this market segment as the services become more affordable. Consequently, the number of mobile subscriptions as well as mobile coverage patterns has continued to demonstrate a positive growth over the period. This trend is likely to continue in future as operators continue employing innovative ways of creating market niche and retaining customers.

The mobile data and internet market experienced an exponential growth on the number of internet users. This is a step forward towards bridging the digital divide in the country with mobile phones being the instrumental platform to accessing internet. The development has greatly contributed in facilitating ease of doing business for small and medium enterprises as operators offer tailor made services for this market at increasingly affordable costs. In addition, internet connectivity has been enhanced by the operationalization of the submarine cables which has led to a reduction to the cost of bandwidth. This in effect has spurred growth in the data market as is witnessed with increased utilization of e-services. Some notable initiatives include the development in e-transactions such as the Mobipay that enables customers buy and pay for goods through the internet, the introduction of e-ticketing services by some bus companies. There is opportunity for further growth with the expected connectivity through an additional cable in the future.

With competitive pressure likely to remain intense among the four service providers, growth in subscriptions is expected to continue to rise further even though it is headed for maturity. This growth is expected to increase as more and more people especially the youth continue to join the social networks like face book, twitters and blogs.

The Information communication technology (ICT) sector continues to experience growth as witnessed in the increase in

subscriptions. The sector is largely driven by the mobile telephony, which continues to dominate the sector. Considering this trend, the coming periods are likely to continue recording growth as operators devise innovative products and services expected to entice subscribers and thus propel this sector even further. The steady growth in the mobile industry sector as recorded by increased subscriptions and traffic is expected to continue with constant technological innovations and continued demand for cellular services. The influential factors in the evolution of mobile services are but not limited to the following; rapid growth in the internet, increasingly data hungry applications, data overtakes voice traffic, users want mobility, prices for voice decrease, huge potential for mobile internet, bleak future for voice revenues and access needed to desktop applications when mobile. Even as operators offer attractive promotions and special offers, this will undoubtedly bring about increased subscriptions and growth in traffic during the coming periods. The mobile money transfer service continues to gain popularity due to its convenience and effectiveness. Owing to its growth pattern, operators will be keen to extend the service to the un-banked population and this is expected to expand this service further.

The ease of subscription coupled by the ease of accessing the service through the mobile phone has enhanced growth in this market segment. Moreover, there is still unexploited capacity and potential in this market segment. Consideration for projects geared towards optimal utilization of this capacity could be valuable as this will ultimately stimulate further growth in this market segment.

C. Recommendations

In the light of the foregoing findings by the researcher, Telecommunication companies should keenly implement the following:

- Concentrate their energies in value added services in order lock in the already existing subscribers and also attract new subscription since the market is headed for saturation.
- Look for ways of improving mobile penetration and coverage while balancing on their returns.
- Research on the different ways of increasing quality of service to significantly new competitive levels.

D. Limitations of the study

Major limitation of the study is lack of available information and previous workings on the topic. There are not enough supportive articles to make an extensive literature review. Also, most of the secondary data obtained and used were scattered. Kenya being a dual-SIM market (where over half the subscribers own three or four lines), counting each SIM card bought could be misleading as well as the fact that the data obtained includes unregistered SIM-cards.

E. Areas of further study

Future research should include forecasting the future of telecommunications firms in Kenya using different methods. Another area of study would be to look at the impact of market maturity on the competitiveness of Kenyan telecommunications companies.

F. Future outlook

The future outlook of the telecommunication is positive as the Commission did the implementation of the Kenya Communications Amendment Act 2008. Telecommunication infrastructure will have a major boost with the completion of the National Optic Fibre Backbone Infrastructure. This key infrastructure is expected to increase bandwidth capacity, in most parts of the country which should have a positive impact on internet diffusion and mobile coverage in rural and remote areas. With the recent focus on local content by data service providers' internet usage in the country is expected to rise. Because of the expected market maturity the telecommunication companies should invest more in value added services and improvement of quality of service.

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Comparison of Classifiers and Statistical Analysis for EEG Signals Used in Brain Computer Interface Motor Task Paradigm

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Abstract—Using the EEG Motor Movement/Imagery database there is proposed an off-line analysis for a brain computer interface (BCI) paradigm. The purpose of the quantitative research is to compare classifier in order to determinate which of them has highest rates of classification. The power spectral density method is used to evaluate the (de)synchronizations that appear on Mu rhythm. The features extracted from EEG signals are classified using linear discriminant classifier (LDA), quadratic classifier (QDA) and classifier based on Mahalanobis distance (MD). The differences between LDA, QDA and MD are small, but the superiority of QDA was sustained by analysis of variance (ANOVA).

Keywords—brain computer interface; electroencephalogram; event related (de)synchronization

I. INTRODUCTION

Brain computer interface (BCI) facilitates a direct communication between brain and an external device. The system - hardware and software - enables humans to interact with their surroundings without involvement of peripheral nerves and muscles, by using control signals generated by brain activity [1]. The interface enhances the possibility of communication for people with severe neuromuscular and motor disabilities. The variety of BCI applications includes: environmental control, locomotion, entertainment and multimedia.

The artificial intelligence system recognize a certain set of patterns in brain signals following the stages: signal acquisition, preprocessing, feature extraction, classification and the control interface. Different methods such as electroencephalogram (EEG), magnetoencephalogram (MEG), positron emission tomography (PET), single photon emission computed tomography (SPECT) are used in measuring and studying the brain activity. The EEG is the most convenient method used in BCI systems: because it is non-invasive, it has relative low costs, the real-time analysis may be performed and can be used in a portable device. EEG based BCIs use a set of sensors that pick up the EEG signals from different brain areas.

EEG signals contain a wide range of frequency spectrum. The oscillatory activity in the EEG is classified according to frequency bands or rhythms: Delta (1-4 Hz), Theta (4-8 Hz),

Alpha and Mu (8-12 Hz), Beta (13-25 Hz), Gamma (25-40 Hz) [2]. Mu rhythm (8-12 Hz) is affected by movements or movement imagery.

Preparing a movement or imagining movement can cause changes in the sensorimotor rhythms (SMR). The SMR refer to oscillations recorded in brain activity concentrated in certain frequency bands [3].

The event-related desynchronizations (ERD) are changes that appear while executing or imagining the movement. ERD starts when the subject begins to imagine a movement and manifests itself as a power decrease in Mu rhythm band. After that, a different phenomenon occurs, event-related synchronization (ERS) - an increase in power when the subject stops executing or imagining a movement.

The phenomenon of ERD/ERS related to motor imagery is stronger for the contralateral hemisphere and weaker in the ipsilateral hemisphere.

In the section II a presentation of the database is completed, how the features are extracted and how the statistical methods are applied. The paper ends with a conclusion and some recommendations based on our results (section III).

II. METHODOLOGY

A. Database description

The EEG Movement/Imagery Database (eegmidb) was downloaded from www.physionet.org [4]. It contains recordings from 109 subjects, who executed real or imagined tasks. The EEG signals were recorded using International System 10-20 with 64 electrodes placed on the scalp. Subjects 43, 84, 88, 89, 92 and 100 were excluded because the contained recordings are not reliable for further processing. We have considered only FC1, FC2, FC3, FC4, C1, C2, C3, C4, CP1, CP2, CP3, CP4 electrodes, reported in the literature for enhancing Mu desynchronization. Every subject performed 14 experimental tasks: 2 runs of 1 minute for relaxation (one with eyes closed and one with eyes open) and 4 runs of 2 minutes for each of the following tasks: opening and closing left/right fist when a target appears on the screen followed by relaxation, imagining opening and closing left/right fist, opening and closing both fists, imagining opening and closing

both fists. In order to implement the proposed methods, there were used the first two sets described above.

Each signal is coded as follows: T0 corresponds to the resting period, T1 corresponds to movement/movement imagery left wrist, T2 corresponds to onset of motion (real or imagined) of the right wrist. The EEG signals are sampled at 160 Hz. There are three trials for wrist movement (named 3, 7, 11) and other three for wrist movement imagery (named 4, 8, 12).

B. Data Processing

Signals loaded from database are filtered with a 8-12 Hz band pass filter corresponding to the Mu rhythm frequency range. No artifact rejection or corrections were performed. We selected segments from the EEG signals (2 s after the stimulus appearance) according to annotation for each mental task (T2, T1) extracting the information corresponding to right/left wrist movement. For the relaxation period (T0) sequences of 2 s following right/left wrist movement are extracted.

The most widely used methods for EEG signal feature extractions are based on frequency analysis, for example discrete Fourier transform (DFT) or power spectral density (PSD). We use a method based on PSD to find the desynchronization during movement. Power spectral densities were calculated for all the useful mentioned channels and for all trials 3, 7, 11 which correspond to right/left wrist movement. The average of these trials was calculated using pwelch function from Matlab with a Hanning window [5]. The same procedure was applied both for computing the PSD during the movement period, denoted by PSD_{MOVEMENT} and for the relaxation period which comes after right wrist movement and left wrist movement respectively, denoted by PSD_{REST}. The resulted value, denoted by ERD, is used to assess the desynchronization/synchronization which appears on the pair of electrodes during right or left wrist movement.

ERD = (PSD_{REST} - PSD_{MOVEMENT}) / PSD_{REST} (1)

The feature vector was formed from each pair of electrodes on the left/right hemisphere in the following way: ERD calculated for right wrist movement for the signal recorded from left hemisphere (FC1, FC3, C1, C3, CP1 or CP3), ERD calculated for left wrist movement for the paired electrode from left hemisphere (FC2, FC4, C2, C4, CP2 or CP4), ERD calculated for left wrist movement for the electrode from left hemisphere, ERD calculated for left wrist movement for the electrode from right hemisphere.

C. Classifiers

Linear discriminant analysis (LDA) is one of the most popular classification algorithms for BCI application, and has been successfully used in a large number of BCI systems such as motor imagery based BCI, P300 speller and steady state visual evoked potentials based BCI [6]. In essence, LDA linearly transforms data from a high dimensional space to a low dimensional space, and finally the decision is made in the low dimensional space, thus the definition of the decision boundary plays an important role on the recognition performance [7].

Linear classifier is suitable for offline and online BCIs. Moreover, LDA, is simple to use and provides satisfactory results whether we are referring to a large or small databases.

Quadratic discriminant analysis (QDA) is closely related to LDA, where it is assumed that the measurements from each class are normally distributed. QDA makes no assumption that the covariance of each of the classes are identical [8]. Although it is not reported and used as much as linear classifier in BCI systems, the quadratic classifier reported satisfactory and encouraging results.

Mahalanobis distance (MD) is a statistical distance function. In mathematical terms, the Mahalanobis distance is equal to the Euclidean distance when the covariance matrix is the unit matrix. The use of the Mahalanobis distance removes several of the limitation of linear classifiers based on Euclidean metric, since it automatically account for the scaling of the coordinate axes, as well as for the correlation between the different considered features [9]. Mahalanobis classifier is simple but at the same time robust and leads to good results, as shown in [10]. Despite its good performance, it is still rarely used in the literature on brain computer interfaces.

Classifiers LDA, QDA and MD were used for all six pairs of electrodes. The steps described above were also accomplished for the trials corresponding to right/left imagery of wrist movement. The classification error obtained for the test set was surveyed for all the subjects, for movement/imagery of movement, pair of electrodes and classifier.

D. Statistical Analysis

A two-way Analysis of Variance (ANOVA) was performed using Statistical Package for the Social Sciences (SPSS) [10] on the error values obtained on movement/movement imagery. The first main factor was CLASSIFIERS with levels LDA, QDA, and MD, while the second main factor was ELECTRODES with levels FC1-FC2, FC3-FC4, C1-C2, C3-C4, CP1-CP2, CP3-CP4. The Levene test was used for testing homogeneity of variances and the Tukey's test was used as post-hoc test at the 2% level of significance.

III. RESULTS

Table 1 shows the means of error rates for all subjects, classifiers and pair of electrodes.

TABLE I. MEAN OF TEST ERROR RATE PERFORMANCE FOR CLASSIFIERS AND PAIR OF ELECTRODES

Table with 8 columns: Task, Classifier, and six pairs of electrodes (FC3-FC4, FC1-FC2, C3-C4, C1-C2, CP3-CP4, CP1-CP2). Rows show error rates for Movement and Movement Imagery tasks using LDA, QDA, and MD classifiers.

For movement, the smallest error of 11,31% was obtained with the quadratic classifier for FC3-FC4, while the largest error 17,62% was obtained with the classifier based on Mahalanobis distance for C3-C4.

For the imaginary of movement there were attained the following errors: the lowest, 12,82%, with the quadratic classifier for FC1 - FC2 and 19,85%, the highest value with classifier LDA for C3-C4. High errors could be explained due to the imperfect contact of the electrodes on the scalp or as the Mu rhythm could not be developed as specified in [11].

On 58% of 103 analyzed subjects the smallest classification errors were obtained for wrist movement, 27% of subjects were able to perform better the imposed task for imagining motor movement than movement. Small errors were achieved for movement as well as imagining the movement for 15% of subjects.

The errors obtained after applying the quadratic classifier were better than those obtained using linear classifier and classifier based on Mahalanobis distance, both for real and imagined motor task. Differences between results for LDA classifier and MD classifier are very small (Fig. 1).

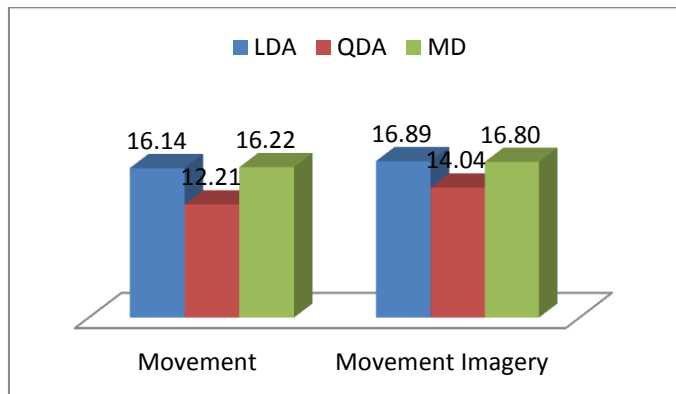


Fig. 1. The error rate for movement and movement imagery using LDA, QDA and MD

We have selected the subjects who attained, even with the quadratic classifier, low classification rates when the EEG signal was passed through a 8-12 Hz band-pass filter. We suppose that these subjects could elicit low or high Beta rhythm instead of Mu rhythm. So, for these subjects only the data were filtered with a 13-18 Hz eighth order Butterworth band pass filter. Filtering on 13-18 Hz was performed on subjects 2, 21, 36, 42, 54, 64, 74, 78, 82, 87, 102, 106. The errors achieved for subject 54 are shown in Table 2. For subject 54, as he attained the best results, the errors decrease significantly if the filter is on 13-18 Hz instead on 8-12 Hz. We can conclude that subject 54 achieved low Beta rhythm. Beta rhythm was also developed by subjects 21, 74, 82, 102. The results show that frequency band other than that of the Mu range may contain useful information. Notable changes on errors were not found for the other seven subjects on 13-18 Hz or 19-26 Hz. In conclusion these subjects could not attain low Beta rhythm or high Beta rhythm.

TABLE II. THE ERRORS FOR SUBJECT 54 WHEN THE SIGNALS ARE BAND PASS FILTERED ON 8-12HZ AND ON 13-18HZ

Subject 54								
Task	Trial	Classifier	Electrodes					
			FC3 - FC4		C3 - C4		CP3 - CP4	
			8-12 Hz	13-18 Hz	8-12 Hz	13-18 Hz	8-12 Hz	13-18 Hz
Movement	3	LDA	38,89	5,56	61,11	5,56	61,11	5,56
		QDA	30,00	5,56	50,00	5,56	55,00	5,56
		MD	38,89	5,56	44,44	5,56	44,44	5,56
	7	LDA	61,11	16,67	61,11	22,22	50,00	27,78
		QDA	27,78	16,67	22,22	22,22	50,00	27,78
		MD	44,44	22,22	44,44	22,22	44,44	33,33
	11	LDA	61,11	5,56	61,11	0,00	61,11	5,56
		QDA	61,11	0,00	61,11	11,11	61,11	5,56
		MD	61,11	11,11	61,11	16,67	61,11	16,67
Movement Imagery	4	LDA	50,00	5,56	61,11	5,56	61,11	22,22
		QDA	50,00	5,56	11,11	5,56	61,11	22,22
		MD	50,00	11,11	44,44	5,56	61,11	22,22
	8	LDA	50,00	50,00	61,11	16,67	61,11	44,44
		QDA	44,44	44,44	61,11	16,67	61,11	44,44
		MD	55,56	38,89	61,11	16,67	61,11	38,89
	12	LDA	50,00	5,56	44,44	27,78	61,11	33,33
		QDA	50,00	5,56	27,78	22,22	52,22	38,89
		MD	50,00	11,11	55,56	27,78	50,00	33,33

TABLE III. THE ERRORS FOR SUBJECTS 2, 74, 87 ON TEST AND TRAINING DATA

Subject	Data	Pair of electrodes					
		FC3-FC4	FC1-FC2	C3-C4	C1-C2	CP3-CP4	CP1-CP2
2	Test Data	16.67	16.98	21.61	19.41	19.44	27.16
	Training Data	16.63	16.05	17.90	24.07	22.84	25.78
74	Test Data	0.93	8.02	4.01	5.25	12.04	10.80
	Training Data	1.85	4.94	9.26	1.87	9.57	11.42
87	Test Data	22.84	23.15	21.91	28.70	19.44	29.94
	Training Data	19.14	21.60	17.90	23.77	19.16	21.30

Table 3 shows the results we had for training and test data for subjects 2, 74 and 87 on pairs of electrodes FC3-FC4, FC1-FC2, C3-C4, C1-C2, CP3-CP4, CP1-CP2. At subject 87 and 2 the errors are higher on test data, then those obtained on

training data and there are consistent for all paired of electrodes. The errors obtained on training data for pairs FC3-FC4, C3-C4 at subject 74 are higher than errors achieved on the others pairs of electrodes.

The ANOVA demonstrated that the use of different classifiers improves the error values. The p-value obtained for CLASSIFIERS was 0.001 for movement and 0.002 for movement imagery. On ELECTRODES the p-value was 0.001 for both tasks.

No interactions between CLASSIFIERS x ELECTRODES was found (p=0.815 for movement and p=0.649 for movement imagery).

Since differences were found in between classifiers, we performed the post-hoc statistical analysis comparison (Tukey test) to determine which classifier is the best. The tests shown that the classification rates obtained for movement/movement imagery with quadratic classifier are higher than those obtained with LDA and MD. At the $\alpha = 0.02$ significance level, there is not enough evidence to conclude that the used electrodes have a significant interaction effect on errors obtained for both tasks.

In Table 4 are depicted the differences between p values obtained with different post hoc tests for classifiers LDA, QDA and DM. Differences between p values obtained with Tukey and Scheffe test are small. The ratio for movement is 0.836/0.850 and for movement imagery 0.965/0.968. Thus, we are confident 98% that with classifier QDA we attained small error that when using LDA and MD classifier. The use of LDA and MD will yield to higher errors since they are similar (Table 4). Although Scheffe procedure is most popular due its conservatism and flexibility, leads to type II errors. Tukey procedure is used mostly for means comparison and leads to type I errors.

TABLE IV. CLASSIFIER COMPARISON WITH POST HOC TESTS SCHEFFE AND TUKEY

Post Hoc Tests	Classifiers Comparison		p value	
			Movement	Movement Imagery
Tukey	LDA	QDA	0,000	0,002
		MD	0,836	0,965
	QDA	LDA	0,000	0,002
		MD	0,000	0,004
	MD	LDA	0,836	0,965
		QDA	0,000	0,004
Scheffe	LDA	QDA	0,000	0,003
		MD	0,850	0,968
	QDA	LDA	0,000	0,003
		MD	0,000	0,006
	MD	LDA	0,850	0,968
		QDA	0,000	0,006

In [12] and [11], using the same dataset relevant results were reported, but also some drawbacks (there are unknown the timing between runs, the age of the subjects or if there are right or left handed subjects).

In another work [13] the classification results were reported only for 30 subjects and were not applied statistical tests.

In most papers regarding BCI research, the classification is performed using a single classifier. A recent trend involves using several classifiers. The combination of multiple classifiers has the advantage of obtaining lower classification errors [6].

IV. CONCLUSIONS

Using power spectral density on the EEG signals contained in EEG Motor/ Movement Imagery Dataset we have studied if desynchronizations appear in the frequency band 8-12 Hz. The classifiers LDA, QDA and MD applied on feature vector were used to determine the classification errors for all six pairs of electrodes.

The results of classification errors vary from subject to subject. The differences among classifiers as LDA and MD are small and reasonable results were attained considering the large database (103 subjects were tested). The used method showed the best performance for the QDA classifier. The performances could be altered because some subjects cannot concentrate well in performing each task. Sometimes they can be absent-minded, ocular or muscles artifacts can occur or they may not have the capacity to imagine movement. Movement and imagining involves sustained mental effort. Also it is important to notice that the recorders contained in database were made on healthy subjects. As some studies revealed that the people who suffer different disabilities can develop Mu rhythm better than the healthy ones, it is possible to get higher classification rates for these persons.

Future work will be focused on a combination of classifiers used in this paper in order to reduce the classification error.

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