

# Stabilizing Average Queue Length in Active Queue Management Method

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**Abstract**—This paper proposes the Stabilized (DGRED) method for congestion detection at the router buffer. This method aims to stabilize the average queue length between allocated `minthre_shold` and `doublemaxthre_shold` positions to increase the network performance. The SDGRED method is simulated and compared with Gentle Random Early Detection (GRED) and Dynamic GRED active queue management methods. This comparison is built on different important measures, such as dropping probability, throughput, average delay, packet loss, and mean queue length for packets. The evaluation aims to identify which method presents better simulation performance measurement results when non-congestion or congestion situations occur at the router buffers in congestion control. The results show that at high packet arrival probability, the proposed algorithm helps provide lesser queue length values, delayed time, and packet loss compared with current methods. Furthermore, SDGRED generates adequate throughput at high packet arrival probability.

**Keywords**—Congestion control methods; GRED; dynamic GRED; random; simulation; active queue management method

## I. INTRODUCTION

The worldwide broadcast of computer networks connects a huge number of devices, from personal computers to multi-branch organization networks [1, 2]. Enormous amounts of data are sent and received between network devices in the form of packets. When several senders send the data over the same intermediary link, packets are stored in the routers' buffer and spend a lot of time waiting for transmitted. However, in view of the buffer size disadvantages in whole network resources [3-5], incoming packets are dropped after the number of packets more than the resource size of the router buffer. Fig. 1 illustrates a possibly congested router buffer. Every packet arriving at the router buffer is considered overflow and dropped as well as causing congestion [6-8]. Of average delay (D) and mean queue length (mql) of packets in the router buffer which also decreases the amount of packets going in the router buffer (T) [9-11].

Enormous congestion control algorithms, such as Gentle Random\_Early\_Detection (GRED) [12], Enhanced Adaptive GRED (EAGRED)[13] and Markov-Modulated Bernoulli Dynamic GRED [6] have been proposed. However, these algorithms have failed to adjust dynamically to provide the best solution based on the mql status.

Generally, the disadvantages of existing congestion control algorithms can be summarized as follows. Existing algorithms

use static probability for packet dropping, and several propose an addition target value that leads to a large number of packet drops when the probability value is high and bursting traffic is present. However, the parameterization problem still exists in most dynamic methods. Bursting traffic causes a heavy congestion signal, which then leads to significant packet drops. Conversely, network performance becomes degraded when the probability of packet dropping is set too low. Specifically, Dp, PL, mql, and D increases, and T decreases. Consequently, a dynamic mechanism is required to implement packet dropping based on the congestion status. This paper proposes an enhance method, Stabilized Dynamic GRED (SDGRED), to address the aforementioned disadvantages and to improve network performance. The latter objective involves alleviating PL and obtaining more acceptable performance measurement results with regard to D and mql when heavy congestion takes place at the router buffers [14].

The paper is summarized as follows. Related work is presented in Section 2. The proposed SDGRED method is covered in Section 3. Section 4 presents the details of simulation experimental environment. The performance results of the developed simulation are discussed in Section 5. Section 6 presents the summary of the proposed paper.

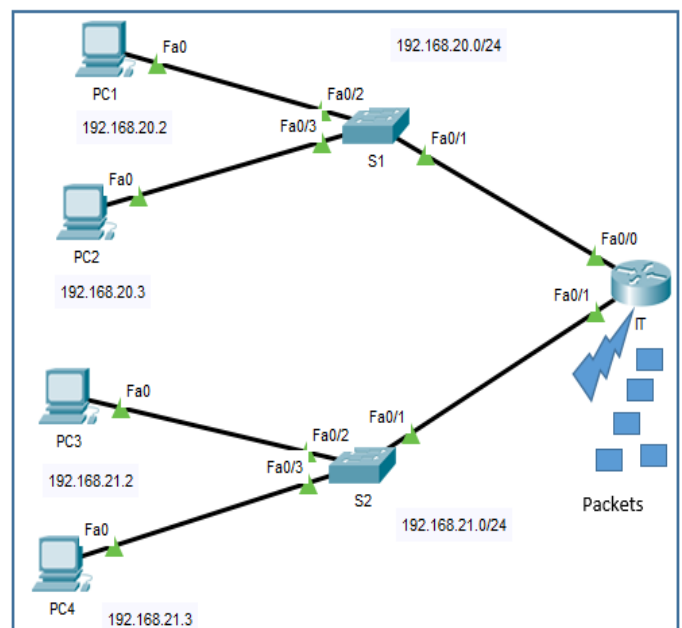


Fig. 1. Congestion in Router Buffer.

## II. RELATED WORK

Several studies have explored controlling congestion and handling the aforementioned problems [15-20]. The Drop-Tail (DT) method [21] aims to control congestion employing a stable router buffer size to optimize queuing delay. The size of the router buffers is set to a maximum and all incoming packets are dropped when the router buffers overflow. There are several disadvantages of DT. Such as, increase the packet delay, decreases the throughput (T), an increase in the packet loss rate, and global synchronization [22].

Average Queue Management Methods (AQM) methods are a solution to overwhelm drawbacks of DT method. Unlike the DT method that starts dropping packets only after the router buffers overflow [13, 14, 23], AQM methods are depend on dropping the packets in the router buffer in early stages. So, early congestion control mechanism notifies the sources sender to start decrease their transmission packets early before the buffers are occupied completely and becomes full. AQM methods control the congestion in the router buffer, so as to increase the throughput, decreases the time delay, decreases the packet loss values, and keeps mql at a lowest value. AQM emerges with an adaptable utilization buffer size. Packet droppings are initiated based on a calculated threshold value to prevent buffer overflow. AQM calculates the current value of aql according to the number of packets then compares it.

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Floyd [27] proposed the GRED to make less some disadvantages in random early detection (RED)[12]. Comparable to RED, the GRED method chiefly purposes to control the congestion in router buffer at an early stage. GRED implements its algorithm by stabilizing the aql at a certain level. GRED uses a familiar approach used by RED in calculating the dropping. Conversely, GRED uses minimum, maximum, and double maximum threshold. Commonly, GRED responds to the arriving packets at router buffer according to the subsequent steps (Fig. 2):

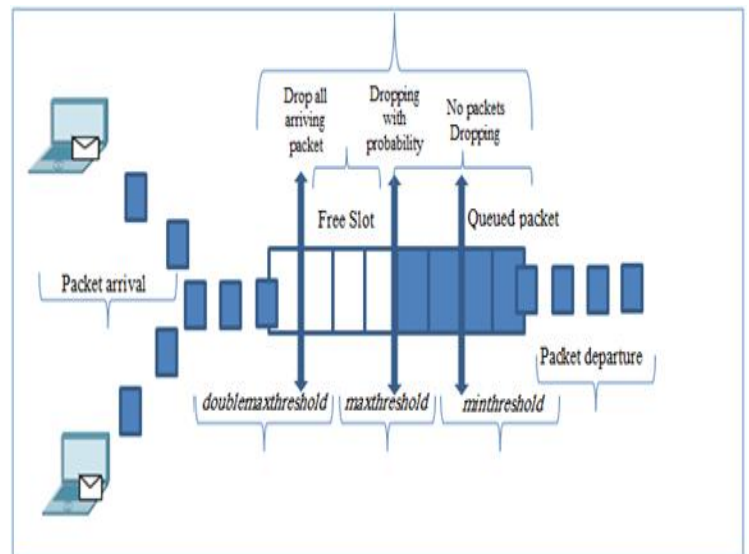


Fig. 2. GRED Buffer.

- When the current value of aql is less than the *minthre\_shold* value, allow receiving packets.
- When the aql is greater than the *minimumthreshold* value and less than *maxthre\_shold* value, the GRED method start drop the packets in the router buffer in random manner, as RED.
- When the aql is reach the *maxthre\_shold* value and less than the *doublemaxthre\_shold* value, the GRED method start drops the packets with based on higher probability scenario.
- Finally, if the aql value is arriving the *doublemaxthre\_shold* value, the GRED method drops every arriving packets and the *Dp* is set one.

However, GRED has several disadvantages. Such as, GRED contains numerous threshold values, GRED parameters are set to exact values to gain satisfactory performance. This causes parameterization problem. And when the current aql value is below the *minthre\_shold* value and heavy congestion occurs in the router buffer, the aql will take a long time to modify; the result the router buffer overflows and becomes full. Therefore, no dropping for packets even with the overfull GRED router buffer.

Dynamic GRED (DGRED) is a development of GRED method. DGRED uses a dynamic *maxthre\_shold* position and *doublemaxthre\_shold* to control the dropping policies mechanism in the router buffer at the early time earlier it overflows[14]. This algorithm aims to stabilize the aql value at the router using an original defined value called Target aql (Taql) that is calculated and set between the *minthre\_shold* and *maxthreshold*. In addition, the proposed DGRED intends to provide better performance results than other AQM methods, such as RED and two of its variants, GRED and AGRED[14]. These results are represented by the results of mql, packet loss, and delay when congestion happens at the buffer, see Fig. 3.

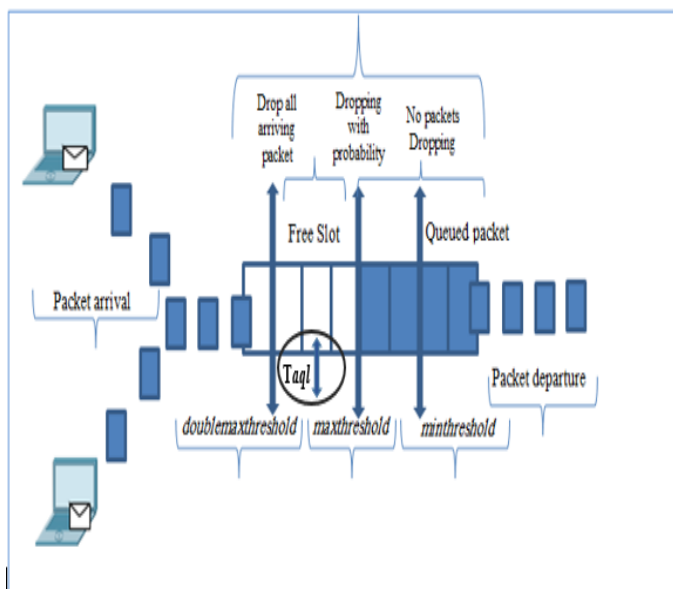


Fig. 3. DGRED Buffer.

DGRED furthermore changes the `maxthre_shold` and `doublemaxthre_shold` parameters setting at the buffer to improve performance measures. DGRED method employs `minthre_shold` and `doublemaxthre_shold` as set in GRED method.

However, DGRED has some limitations. DGRED involves several threshold values and `Taql`, which means using parameters to control the congestion in the router buffer (parameterization).

### III. PROPOSED SDGRED METHOD

Fig. 4 shows SDGRED's processing stages. The parameter setting initialization step (Step 1) ensures that parameters are actually specified when the packets reach the router buffer. SDGRED method uses the `minthre_shold` and `maxthre_shold` values as that in DGRED method [14]. The `doublemaxthre_shold` in SDGRED method is considered the same value as that in DGRED[14], see Fig. 5. The initial value of `aql` is set zero and the counter sequence value starts from -1.

The SDGRED method then receives packets (Step 2) using a Bernoulli model,  $\epsilon \in [9]$ ,  $n = 0, 1, 2, 3, 4, 5 \dots$ , wherever  $n$  refers to the arrival packets number in the router buffer in specific slot  $n$ . the Bernoulli process is appropriate when the buffer has a static length slot.

SDGRED then observes the queue status in the router buffer (Step 3) and calculates the `aql` value depend on status the buffer either contain packets or not contain packets, as shown in Fig. 6. Thus, in the case of empty router buffer queue, the `aql` value is considered according to idle time ( $n$ ) and computed using Equation (1). Meanwhile, in the case of router buffer queuing, the `aql` is computed using Equation (2).

$$average\ ql = average\ ql \times (1 - average\ w)^n \quad (1)$$

$$average\ ql = average\ ql \times (1 - qw) + qw \times q\_inst \quad (2)$$

Next (Step 4), the SDGRED method matches the `aql` value with the thresholds position values and subsequently updates

`maxthre_shold` and `doublemaxthre_shold` positions in the router buffer to increase network performance (Fig. 7). Both `maxthre_shold` and `doublemaxthre_shold` values set according to the `aql` value.

In Fig. 7, the `maxthre_shold` and `doublemaxthre_shold` values increased and decreased around the `minthre_shold` by Equations (3) to (5) to prevent congestion at the router buffers. Thus, the `aql` value stabilizes around the `minthre_shold` and prevents the saturation of router buffers. As a result, fewer packets are dropped. Furthermore, the calculations can cause changes in `aql` value in a slow mode. Therefore, the Equations (3) to (5) are derived.

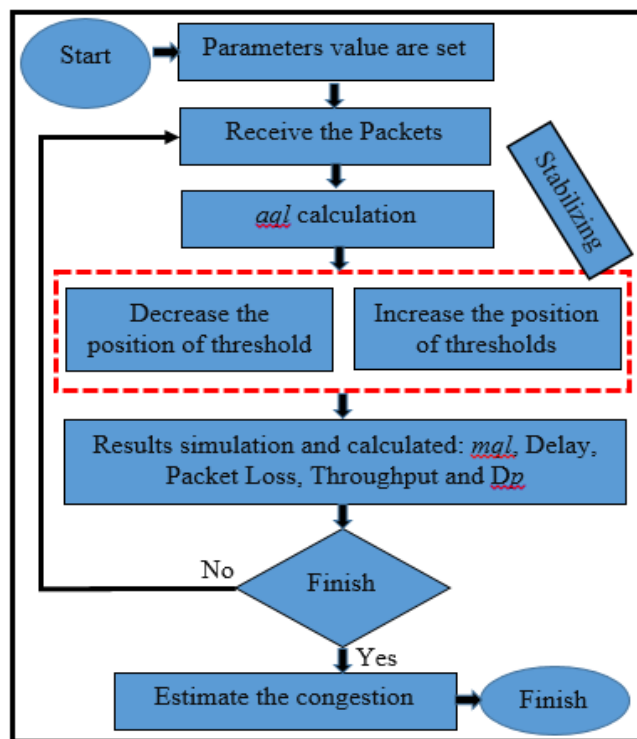


Fig. 4. SDGRED Stages.

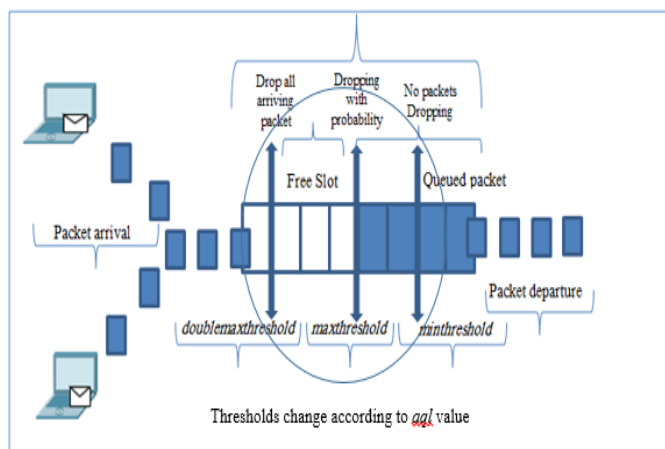


Fig. 5. The Proposed SDGRED Buffer.

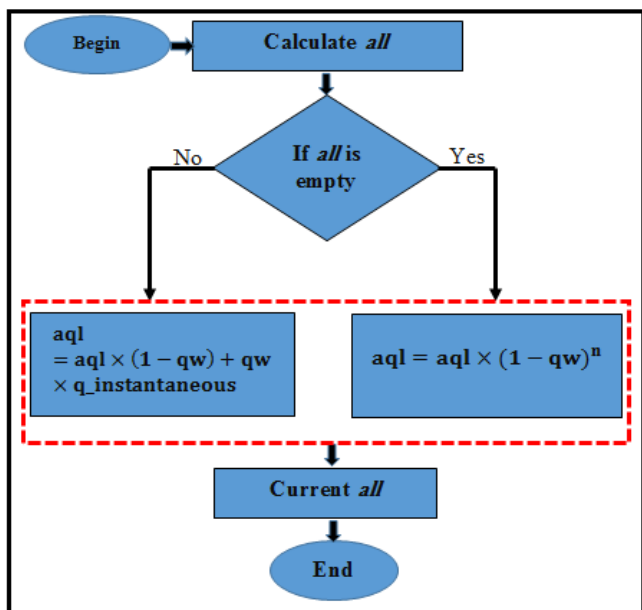


Fig. 6. Average Queue Length Status.

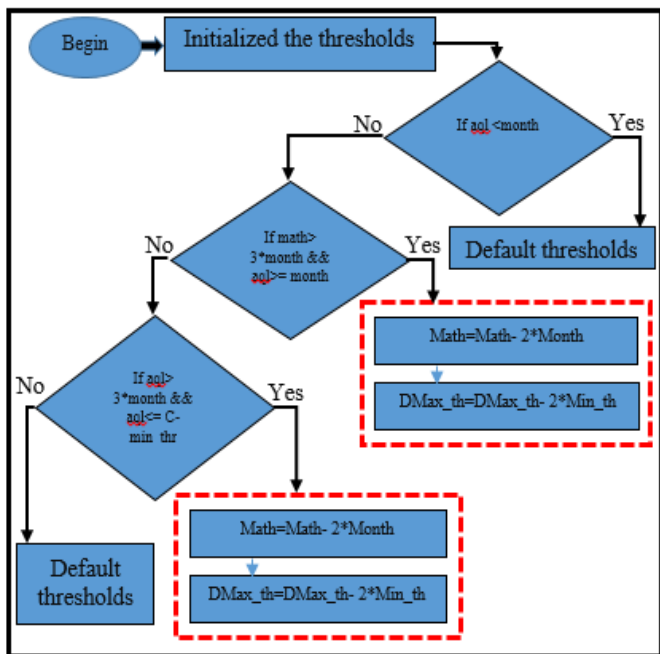


Fig. 7. Thresholds Stabilizing Stages.

As such, when the aql value is below min\_threshold, no change occurs and the min\_threshold, maxthre\_shold and doublemaxthre\_shold values will initialize [27]. Conversely, when the aql value is below the minthre\_shold multiply two according Also maxthre\_shold is reach greater than or equal to the position of minthre\_shold multiply three, then the maxthre\_shold and doublemaxthre\_shold values change using Equations:

$$\text{maxthreshold} - 2 * \text{Minthre\_shold} \quad (3)$$

$$\text{Doublemaxthreshold} - 2 * \text{Minthre\_shold} \quad (4)$$

$$\text{maxthreshold} + \text{Minthre\_shold} \quad (5)$$

Thus, the aql value arises rapidly and stabilizes at the min\_threshold. Also, if the aql is greater than the minthre\_shold multiply three and less than or equal to the buffer capacity min\_threshold, the maxthre\_shold and double maxthre\_shold values will set as shown by Equation. Thus, they become the same and prevent the double maxthre\_shold value to go over the buffer capacity. Subsequently, the maxthre\_shold and doublemaxthre\_shold values increase to push the aql near the minthre\_shold and decrease the probability the router buffer becomes full and over flows. In the last, in a case none of previous scenario happen, the maxthre\_shold and doublemaxthre\_shold is set to the same values as in the DGRED method [22].

(Step5) of the SDGRED method, the congestion is assessed and packet dropping is applied. aql plays a main role in congestion estimation according to dropping polices. In case the aql value is not reach the min\_threshold, no event for congestion is presented at the SDGRED router buffer and no packet is dropped. In addition, Dp is fixed to zero and C is fixed to-1. Hence, no packet is reached to the boundary of threshold. If the aql value is between the minthre\_shold and maxthre\_shold values, the SDGRED router buffer operates as DGRED for dropping the arrival packets. Dropping packets based on increasing C by 1 and calculating Dp for arriving packets. If the aql value is between the doublemaxthre\_shold and maxthreshold, the SDGRED router buffer starts drop the incoming packets based on DGRED method, which involves initializing the C value and set one and calculating Dp for current arriving packets. Lastly, if the aql value is reach the doublemaxthre\_shold value, the proposed SDGRED router buffer drops every arriving packet with Dp equal 1 and sets C to zero. Subsequently, in case the SDGRED router buffer becomes empty, the value of idle time is set to current time directly.

#### IV SIMULATION

GREED, DGRED, and the proposed stabilize DGRED are simulated depend on a discrete time queue model which uses a time as a slot [28, 29]. Each slot time may contain packet arrival (alpha) and packet departure (beta). Simulation is implemented by applying the compared methods in a network environment involving a lone router buffer hop. Particularly, both packet arrival and departure are implemented in single hope on a first packet arrival first packet departure basis. GREED, DGRED, and SDGRED simulations are applied in Java with i5 processor device, 1.68 GHz and 8 GB RAM. In this simulation, the probability value for both alpha and beta for the router buffer in a specific slot time is called alpha and beta, respectively [23, 29].on the other hand, the Packet arrivals and packet departures are demonstrated using a Bernoulli process and a geometrical distribution, respectively [29].

#### IV. EVALUATION RESULTS

The performance results of the SDGRED method is compared with DGRED and GREED AQM methods. The performances are implemented in simulation environment 10 runs, each run getting different seeds value as an input to the random number producer. This scenario eliminates likely bias in the output performance results and yields confidence intervals value. The performance results are calculated after the



system becomes stable to collect the results which means a steady state.

For the parameters are set in GRED, DGRED, and the proposed SDGRED are introduced using equal parameters at most. In order, to make congestion and non-congestion situations at the router buffer, the packet arrival was set to the following values[7].0.18,0.33, 0.48, 0.63, 0.78 and 0.93 respectively; each value of them goes to generate congestion or non-congestion station. The buffer size room was set 20 packets to guarantee the congestion at small buffer sizes. A total slot was set to 2000000 were used in the simulations. The minthre\_shold is set 3, the maxthre\_shold is set 9, doublemaxthre\_shold is set 18, Dmax, is set 0.1 and qw is set 0.002, as recommended in DGRED[14]. Table I lists all the utilized parameters. The simulation performance results are stately using numerous performance metrics. Such as, Throughput, Delay, mql, packet loss, and dropping probability, which are discussed in the following subsection.

TABLE I. PARAMETERS SETTING

Parameter	DGRED	DGRED	SDGRED
alpha	0.18,033,048,0.63,0.78,0.93	0.18,033,048,0.63,0.78,0.93	0.18,033,048,0.63,0.78,0.93
beta	1/2	1/2	1/2
Buffer size	20	20	20
Q_w	0.002	0.002	0.002
D_max	0.1	0.1	0.1
# of slots	2 millions	2 millions	2 millions
Mint_hreshold	3	3	3
Max_threshold	3*min	3*min	3*min
Double_maxthreshold	2*max	2*max	2*max
Target aql	parameter	-----	dynamic

Mean Queue Length, Throughput, and Delay Results.

Respectively, Fig. 8, 9 and 10 explain the output performance results for GRED, DGRED, and the proposed SDGRED using different probabilities of packet arrivals as mention above. Specifically, Fig. 8 shows the mql and the probability of packet arrival.

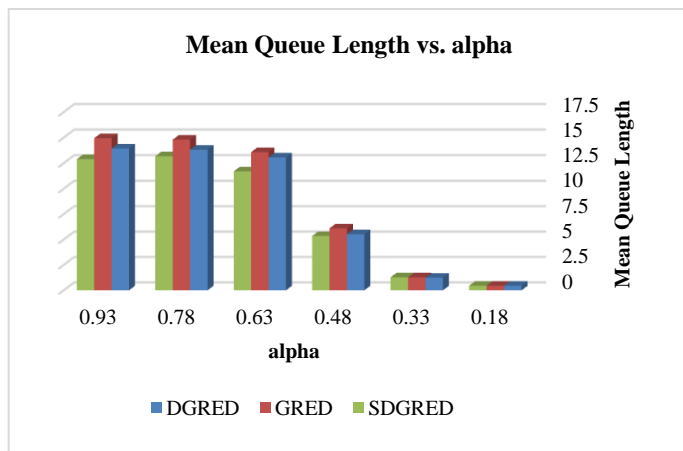


Fig. 8. Mean Queue Length.

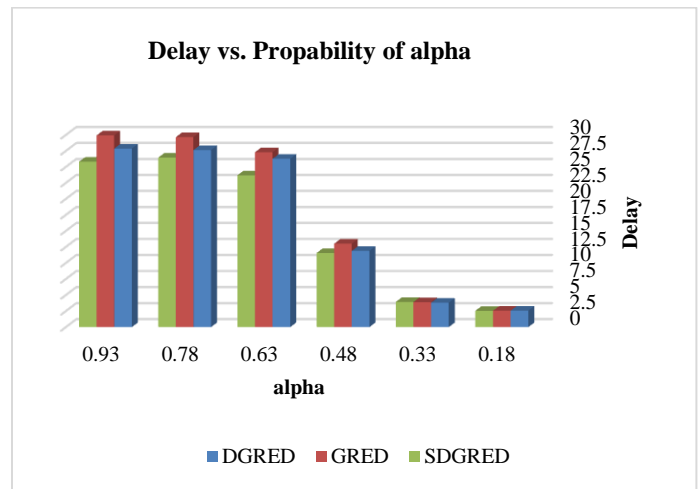


Fig. 9. Delay Performance Results.

The mean queue length for all methods and SDGRED method is the same up to a certain value of the probability of alpha 0.18, 0.33 and 0.48. Such a small probability value reasons bright congestion at most because the probability of packet departure was set 0.5 greater than that of alpha ( $a > B$ ). So, all compared methods gain satisfied and stable mean queue length values. On the other hand, for a higher probability values, such as, 0.63, 0.78 and 0.93 congestion is more likely to occur at the router buffers. Thus, the mean queue length of the AQM methods arises exponentially. In such a case, the proposed SDGRED performs better than the DGRED and GRED methods because fewer packets are dropped and the router buffer space available for new packets arrival.

Fig. 9 illustrates a comparison of the delays in all algorithms. Although DGRED shows good performance in terms of the average delay, the proposed SDGRED performs better because of the fewer dropped packets in SDGRED.

Finally, Fig. 9 shows the throughput performance measure in all the packet arrival probabilities were set. The proposed SDGRED and compared methods gain the same throughput results either light congestion or heavy congestion, the packets arrival probability are set to 0.18, 0.33, and 0.48 which means lower probability or higher than that of packet departure, such as, 0.63, 0.78 and 0.93. Fig. 10 refers a probability of packet arrival arrive 0.18, 0.33 and 0.48 increases to arrive to the packet departure value. On the contrary, when the alpha arrives the value of beta, all the compared methods stabilize at the packet departure probability which equals 0.5 when congestion happens.

#### A. Packet Loss and Dp

The proposed SDGRED method is likewise compared with the DGRED and GRED methods in regards of PL performance measures and DP performance measures to display the amount of dropped packets in the buffer. The results of PL and DP are computed after the simulation becomes stable and steady. The method simulations are run 10 times with various random seeds and the mean is determined. The results of GRED, DGRED, and the proposed SDGRED algorithms in means of PL and DP are clarified in Fig. 11 and 12, in that order.

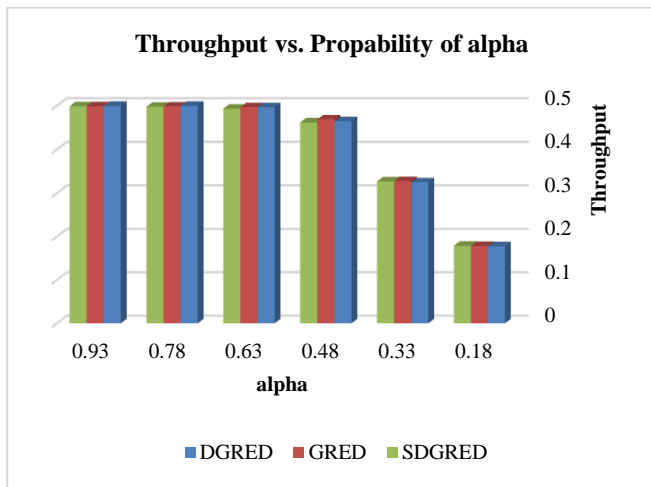


Fig. 10. The Throughput.

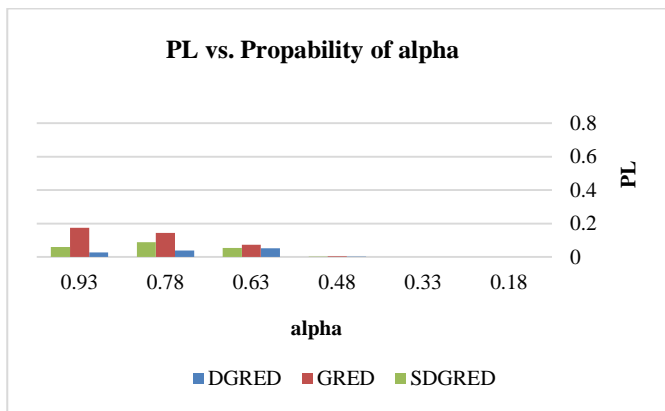


Fig. 11. Packet Loss Result.

In Fig. 11, GRED, DGRED, and the proposed SDGRED algorithm marginally produce the same PL performance result when the beta probability is greater than that of alpha. The DGRED introduces better PL performance at heavy congestion because the router buffer overflows earlier compared with those in the GRED and SDGRED methods.

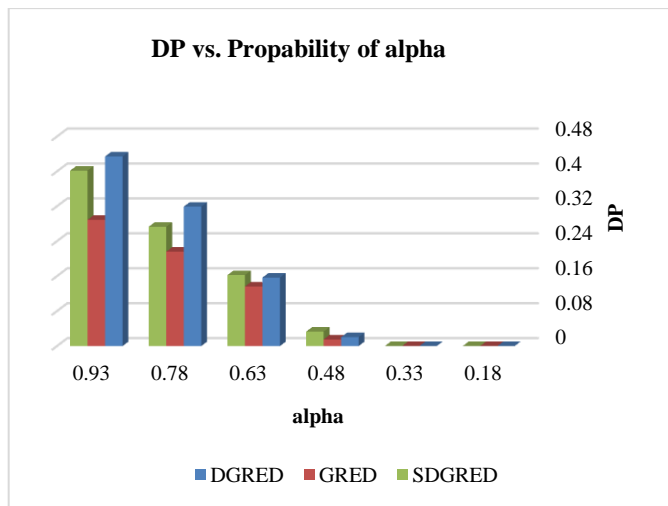


Fig. 12. Dropping Probability.

Fig. 12 shows that for the same reason, the proposed SDGRED algorithm evidently drops more packets when the beta probability is lower than that of alpha.

Therefore, the proposed method reveals the following improvements:

- GRED, DGRED, and the proposed SDGRED methods the same performance measure results when the alpha equals 0.18, 0.33, and 0.48.
- The SDGRED method offers a marginally better mql and Delay than the DGRED, and GRED methods when the alpha arrive to the 0.63, 0.78 and 0.93. In addition, when the alpha less than 0.5, the GRED, DGRED, and the proposed SDGRED methods gain similar T performance results.
- DGRED method slightly outperforms the SGRED and GRED methods for PL when heavy congestion. Moreover, at such values of packet arrival probability, SDGRED drops fewer packets (Dp) at their router buffers.

## V. CONCLUSIONS

The current paper proposed an enhanced AQM method depend on the DGRED called the SDGRED. The proposed SDGRED aims to keep the aql between the minthre\_shold position and doublemaxthre\_shold position by changing the maxthre\_shold and doublemaxthre\_shold positions according to current aql value. This aql change helps stabilize the aql at minthre\_shold position in order to prevent the congestion. SDGRED employs maxthre\_shold and doublemaxthre\_shold positions in adaptive manner to keep the aql value arround the minthre\_shold value, which may lead to fewer packet losses and queuing delay. The SDGRED technique is compared with the GRED and DGRED methods with the following performance measures such as, T, mql, D, PL, and Dp, to present which method offers better performance result in regards of packet arrival probability. The results show the SDGRD method is competitive to the compared methods.

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