# Using a Fuzzy-Bayesian Approach for Predictive Analysis of Delivery Delay Risk 

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#### Abstract

Although one of the major roles of delivery logistics activities is to ensure a good quality of customer service, certain risks such as damage, delay, return of transported goods occur quite often. This makes risk control and prevention one of the requirements of transport supply chain quality. The article focuses on the analysis of the risk of delay, which is often considered fundamental for the quality of service and as a center of additional costs related to the violation of time windows. Such a risk can harm the image of a supplier, which can even lead to the loss of customers in case of recurrence. The aim of the following case study is the development of a fuzzy-bayesian approach that anticipates, by predictive analysis combining Bayesian networks (BNs) and Fuzzy logic, the possible delays affecting the smooth running of a delivery operation. The results of the implementation of the late delivery risk prediction model are validated by verifying three axioms. In addition, a sensitivity and scenario analysis is performed to validate the model and identify the parameters that have the most adverse impact on the occurrence of such a risk. These results can help carriers/transport providers to minimize potential late deliveries. In addition, the developed model can be used as a basis for different types of predictions in the field of freight transport as well as in other research areas.


Keywords—Delivery logistics; risk management; predictive analysis; bayesian network; fuzzy logic

## I. InTRODUCTION

On-time delivery is often considered as a performance indicator in the field of freight transportation [1]. However, any delay in goods delivery to their destination can harm the activities of the actors involved (shipper, carrier, warehouseman, and final customer) and affect their profitability. Therefore, measuring the risk of delay in advance enables reliable decisions to be made when planning deliveries. Consequently, the effect of such a risk can be reduced or even eliminated. This study focuses on the analysis of delivery delay to assist transportation companies in making decisions and optimizing their planning. Despite, the development of a delay risk prediction model is hampered by the unavailability of data. With this in mind, this paper contributes by implementing a fuzzy-bayesian approach to overcome the problem of missing or unavailable data.

The occurrence of delay in freight transport operations is influenced on the one hand by external factors such as road events (accidents, congestion, and weather conditions). On the other hand, by internal factors related to carriers' decisions in terms of resource selection and delivery planning [2]. This
paper has studied all of these elements, and it has designed a predictive model integrating the different cause-effect relationships between several factors (internal and external) impacting on-time delivery. For this, it opted for BNs [3] thanks to its advantage of modeling, probabilistic reasoning of uncertain systems [4], and causal analysis.

The article is structured as follows: an overview of the literature related to delivery delay and the application of BNs in the transportation domain is given in Section II. The construction of the fuzzy-Bayesian model and its validation are presented in Section III. Section IV provides a discussion of the results obtained. Finally, the conclusion and further research are covered in Section V.

## II. Related Work

In this section, we provide a brief overview of literature regarding our context of study, namely delayed deliveries, and for Bayesian network applications in transportation field.

## A. Delayed Deliveries

Delayed deliveries mean goods arriving at their destination out of schedule. According to ATRI (American Transportation Research Institute), in 2016, trucking operations in the U.S. experienced about 1.2 billion hours of delays alone due to traffic congestion. This number of delays generates $\$ 74.5$ billion in additional operational costs [5]. Because there are other causes of delay besides congestion, these additional costs continue to rise.

According to [6] various factors can disrupt delivery reliability, among them personnel issues, vehicle breakdowns, and poor planning. This means that resource selection by checking vehicle conditions and driver performance in addition to the adequacy of planning have a significant effect on speed of service. Furthermore, other external factors such as accessibility to delivery points, accidents, unforeseen events (public works), and methodological conditions [6]-[8] can cause further delays.

The occurrence of delay largely influences [9]-[12]:

- Additional costs: these costs are typically related to a delay penalty, and vehicle operating costs such as maintenance and vehicle rental in the case of private fleet use. As well as driver-related costs, that include salary and benefits. In addition, delay can lengthen the storage period, resulting in inventory holding costs.
- Warehouse productivity: arriving late at the warehouse may result in overlapping deliveries. This will influence the availability of unloading bays and labor as well as overloading the workforce to wait for late deliveries.
- Customer satisfaction: late deliveries can affect the operations of the consignees. This will have a significant impact on the customer relationship. As a result, customers find themselves in a situation of frustration. In case of recurrence, this situation exposes suppliers to the loss of customers.
- Loss of opportunity to consolidate shipments: the occurrence of delays contributes to the lack of opportunity to consolidate shipments due to the uncertainty of meeting delivery deadlines.
- Carrier profitability: this is generally affected by the additional costs incurred, the damage to the carrier's image due to the loss of customers and the extra time generated which reduces the opportunity to make more deliveries.

The concept of predicting the risk of late delivery is generally studied in the context of improving service quality. In the literature, the prediction of such risk is performed using several techniques from artificial intelligence.

Keung et al. [13] have opted for machine learning methods such as KNN, and ANN to predict shipment delays. The authors [14] used Random Forest and SVM for on-time delivery prediction. Berrones-Sanz [15] also proposed a model for on-time delivery prediction using logistic regression. In order to predict on-time delivery violation, [16] relied on ANN machine learning technique. As for [17], they proposed a neural network-based model to anticipate delivery time.

In addition, BNs are among the most popular prediction methods in various research areas [18]. This paper exploits the potential of BNs in risk prediction to anticipate the occurrence of delay in a delivery operation.

## B. Applications of BNs in the Transportation Field

BNs are applied in several domains: diagnosis (medical and industrial), risk management, spam detection, fraud detection, data mining, and text mining, etc.[19]. In the transportation domain, BNs are used for different types of prevention. Gregoriades and Mouskos [20] used BNs to quantify the risk of accidents in order to locate black areas. The authors [21] developed a bayesian model for the identification of features affecting the safety of motor carriers. Zhu et al. [22] presented a bayesian approach for contextual (e.g., dynamic traffic information) or non-contextual (e.g., instantaneous driving speed) evaluation of driving behavior. As for [23], they modeled drivers' vehicle use behavior according to time of day. The use of BNs also extends to other transportation axes, namely traffic congestion prediction [24], [25] as well as freight demand prediction [26].

## III. Modeling the Risk of Late Delivery using a FUZZY-BAYESIAN APPROACH

A BN is "a graphical probabilistic model consisting of a set of nodes (variables of interest in the domain) and arcs (causal phenomena). In addition to a set of local probability distributions (network parameters)" [3], [27], [28]. A BN allows modeling the effect of a fact or an uncertain event on another via the representation of the causal relationship between those events [29]. In this case, an arc from X to Y can be interpreted as ' X causes Y '. Fig. 1 shows that the knowledge gained about the overlay of fragile products determines the knowledge about the damage of goods.


Fig. 1. Example of a Causality Representation.
The study is based on exhaustive bibliographical research, in addition to a survey of experts, in order to identify all the parameters (factors) which can hinder the delivery of a good to its destination in time. As well as the schematization of the dependency relations between these parameters, in order to build the structure of the Bayesian network. The approach followed introduces a methodology for modeling and evaluating the risk of late delivery using BNs by following these steps:

Definition of the BN structure: Determining the relationships between nodes allowed us to design a causal graph based on a three-level architecture.

- The first level represents the input or feeder nodes that have an indirect effect on the risk of delay; they fall into five categories detailed in Table I;
- The second level consists of the intermediate nodes that represent the various intermediate cause factors (direct causes, or cause-effects) that lead to the impact factors encapsulated in the third level (final impacts);
- The third level contains the final impacts that define the factors that directly and negatively influence the arrival of goods at their destination on time.

Generate conditional probabilities of intermediate effects and final impacts: The generation of conditional probability tables will be made using Sugeno's fuzzy inference implementation.

Model validation: This step consists of relying on Bayes theory and posterior probabilities relating to intermediate effects and final impacts, in order to study the effect of a state linked to an input parameter on the envisaged risk. In addition, sensitivity analysis and partial validation are performed to validate the model.

## A. Definition of the BN Structure

The construction of the Bayesian network architecture can be done in two different ways:

- Objective methods: by using a database to apply the structure's learning methods.
- Subjective methods: by gathering knowledge from experts in the field, through written questionnaires, individual interviews or brainstorming sessions.

The first approach necessitates a large quantity of data. and it may establish dependencies or independencies between some variables that are inconsistent with the experts' opinions [30]. For this reason, researchers prefer the use of the second approach where experts are involved to verify the causal links between the network variables. [31]. In the literature, several researchers have relied on expert knowledge among them [31][35].With this in mind, the article used the subjective method.

Based on a survey of experts in the freight transportation field and a literature review of the various factors that drive the occurrence of delay risk, a set of network input parameters are identified and presented in detail in Table I. In addition to the intermediate effects and final impacts presented in Table II. The survey consisted of two questionnaires, the first was conducted to verify and validate the identified variables and the second to establish the causal relationships between the variables.

After identifying the variables (Tables I and II) that will constitute the nodes of the graph and studying the causal relationships between them, the structure of the Bayesian network is developed and illustrated in Fig. 2.

## B. Generation of Conditional Probabilities of Intermediate Effects and Final Impacts

After building the Bayesian network structure, the next step is to compute the conditional probability tables (CPT) for each variable. These CPTs can be computed based on the knowledge of the experts or using learning algorithms from a database. Although there is no more database in the literature adapted to the parameters identified to build the graph structure, the article is oriented towards the use of subjective methods.

Since the number of conditional probabilities in the developed network is 1032, it is difficult to rely on expert knowledge to evaluate such a large number of probabilities[36]. In fact, in the literature, many researchers
have developed models to lower the number of CPTs of a BN. As an example, causal interaction models that have attracted the interest of several researchers such as [37]-[41]. One of the most widely used models is the Noisy-OR model introduced by [39] which allows for the specification of non-deterministic interactions between the parents associated with an effect [42].

In addition, other methods such as fuzzy logic [43] allowing the reduction of numbers of questions asked to experts and the generation of probability tables [2], [44], [45] .With this in mind, the paper relied on this method to first express the experts judgments by fuzzy rules, and then generate the conditional probability tables by a fuzzy inference mechanism. These fuzzy rules are of the type 'If the driver's performance is bad then the occurrence of the accident is high. Here the value of "high" for the accident occurrence is qualitatively represented by a linguistic variable expressed in natural language. For the different rules, the accident occurrence node can be translated into one of the following values: low, medium, high. In addition, for the different nodes of the graph, their influences are revealed by three linguistic values (states) represented in Table III. Since the quantification of these linguistic variables oscillates in interval 0.1 , the article opted for the expression of these values in fuzzy form to ascertain the degree of each node's membership in all its fuzzy subsets. As an example, the accident occurrence node is high with $90 \%$, medium with $8 \%$ and low with $2 \%$.

The implementation of the approach adopted for generating conditional probability tables is done in three steps:

- Definition of fuzzy variables, their associated linguistic values(variable whose values are qualitative and represent natural language expressions [62] and their membership functions;
- Determination of fuzzy rule bases: a base of "if-then" rules, is used by the "fuzzy inference system" in order to translate the input variables into output [62];
- Development of inference mechanism that forms conclusions based on the fuzzy rules and the input data [63].


Fig. 2. The Structure of the Bayesian Network Modeling the Risk of Delay of a Delivery.

TABLE I. DESCRIPTION OF THE INPUT PARAMETERS OF THE CAUSAL GRAPH

| Variable class | Variable name | Description |
| :---: | :---: | :---: |
| Parameters related to the road | Road design | It refers to the geometric nature of the road, such as the number of lanes and direction of traffic. [46]. |
|  | Lighting | Lighting conditions (artificial light, daylight, darkness, twilight) have a considerable effect on the occurrence of road accidents, due to the adaptation of speed with visibility conditions [47]. |
|  | Road cleaning after accident | Improper cleaning of accident sites can result in the vehicle skidding due to the presence of body fluids, fuel and other debris. |
| Traffic parameters | Signage | Traffic signal control considers the control of traffic signals and the existence of stop sign and yield sign [48] |
|  | Weather conditions | Weather conditions can disrupt driver capabilities, pavement friction, road infrastructure conditions, and vehicle stability and maneuverability, due to reduced visibility, extreme temperatures, precipitation, high winds, and lightning [49]. As a result, they affect traffic demand (carriers postpone or cancel planned delivery operations), traffic safety (accident rates), and traffic flow relationships (changes in the fundamental traffic flow variables, volume, speed, and density influence the capacity of a road system) [50]. |
|  | Occurrence of events that block/slow traffic | Traffic can be disrupted by the occurrence of a variety of events, including: <br> Unexpected events such as road accidents, vehicle breakdown in the middle of the road, land subsidence and public works [51]; <br> Irregular social events such as political demonstrations, diplomatic visits [51], sporting events; Regular events such as festive events (religious, national or international holidays) and vacation departure; In addition, the delivery period also influences traffic. Delivery during peak hours can slow down traffic. |
| Parameters related to personnel (drivers, planners, ...) or planning systems | Driver behavior | Driver behavior is considered one of the major sources of traffic accidents [52]. <br> These behaviors include failure to observe speed limits, safety distance, and poor vehicle handling that manifests itself in hard braking, and hard acceleration, especially when visibility is reduced, and when climbing hills [53]. |
|  | Driving style | A driver's habitual driving style that includes calmness behind the wheel, level of attention contribute to traffic accidents [54], [55]. |
|  | Driver condition | The poor condition of drivers is often due to fatigue, alcohol consumption, negative emotions (worries and fear of arriving late), drowsiness, headaches, respiratory illnesses, and fever [56]. |
|  | Number of exchanges | The increase in the number of exchanges resulting from indirect deliveries leads to more loading/unloading operations [57], and therefore an increase in the risk of delay due to uncontrolled/estimated time at the exchange points. |
|  | Departure time | A travel time estimate is said to be accurate if it could help improve the quality of service by delivering the goods on time [58]. For this, the departure time must be sufficient to cover the planned route within the required time window. |
|  | Resource allocation | Personnel, vehicle condition (breakdown), and delivery points are among the factors that cause delay to occur [6]. Therefore, optimal allocation of resources (vehicles, warehouses, personnel, etc.) to routes helps to reduce the risk of delay. |
| Vehiclerelated parameters | Vehicle condition | Vehicle condition is one of the causes of accidents [59]. Poor physical condition of the vehicle can cause vehicle breakdown and hence the occurrence of delays. In addition, negligence in checking the administrative condition of vehicle can be the cause of vehicle ticketing. |
| Parameters related to delivery areas (warehouses) | Availability of delivery bays | The lack of adequate delivery bays for different vehicle sizes leads to long queue [60]. In this case, drivers try to park their vehicles far away or illegally near the delivery site. This leads to long queue. |
|  | Resource availability | The lack of human resources in the delivery areas is one of the factors that lead to long queue[60]. Similarly, the lack of material resources (handling equipment, forklifts, etc.) can aggravate this problem. |
|  | Internal events | Internal events such as strikes over working conditions can slow down or block access to delivery areas. |
|  | Scheduling of arrival times | Synchronizing inbound and outbound delivery operations within a warehouse requires reliable arrival times [61]. Lack of scheduling of arrival times (delivery deadlines) with carriers can cause overlapping operations of multiple deliveries, subsequently resulting in long queues. |

TABLE II. Presentation of Intermediate Effects and Impacts on Delay

| Intermediate effects |  | Final Impacts |
| :---: | :---: | :---: |
| - Road visibility <br> - Vehicle skidding <br> - Condition of the road infrastructure <br> - Spillage of substances <br> - Congestion <br> - Occurrence of ticket | - Road environment condition <br> - Driver performance <br> - Queue <br> - Parking <br> - Occurrence of accidents <br> - Occurrence of breakdown | - Additional travel time <br> - Accessibility to destination points <br> - Relevance of planning <br> - Occurrence of delay |

TABLE III. States of the Bayesian Network Nodes

| Nodes | Linguistic values |
| :---: | :---: |
| Road design | Good, medium, bad |
| Lighting | Good, medium, bad |
| Fog | Low, medium, heavy |
| Road visibility | Good, medium, bad |
| Condition of the road infrastructure | Good, medium, bad |
| Road cleaning after accident | Appropriate, medium, inappropriate |
| Spillage of substances | Low, medium, strong |
| Vehicle skidding | Low, medium, significant |
| Weather conditions | Normal, medium, extreme |
| Occurrence of events that block/slow traffic | Low, medium, high |
| Signage | Good, medium, bad |
| Congestion | Low, medium, high |
| Road environment | Good, medium, bad |
| Vehicle condition | Good, medium, bad |
| Driver performance | Good, medium, bad |
| Driver behavior | Good, medium, bad |
| Driving style | Good, medium, bad |
| Driver condition | Good, medium, bad |
| Occurrence of accidents | Low, medium, high |
| Occurrence of breakdown | Low, medium, high |
| Occurrence of ticket | Low, medium, high |
| Additional travel time | Low, medium, high |
| Number of exchanges | Low, medium, high |
| Resource allocation | Good, medium, bad |
| Relevance of planning | Good, medium, bad |
| Estimated departure time | Good, medium, bad |
| Scheduling of arrival times | Good, medium, bad |
| Occurrence of internal events | Low, medium, high |
| Resource availability | High, medium, low |
| Availability of delivery bays | High, medium, low |
| Queue | Fast, medium, slow |
| Parking | Very close, close, far |
| Accessibility to destination points | High, medium, low |
| Occurrence of delay | Low, medium, high |

To better assimilate our proposed approach, we explain CPTs generation for 'Congestion' node. In this case, the inference mechanism aims at determining the probabilities of the occurrence of congestion with respect to the states of the nodes: Signage, weather conditions, occurrence of events blocking/disrupting the traffic.

The membership function used for the different nodes of the graph is Gaussian, as it provides less error compared to other triangular and trapezoidal functions [64]. An example of the description of the membership function for the weather variable is provided in Fig. 3.


Fig. 3. Membership Functions for the Weather Variable.
After defining the membership functions for the congestion nodes and its antecedents, subsequently, a fuzzy rule base is determined to evaluate the variation of the congestion node with respect to the states of its parent nodes or its causes. This fuzzy rule base is detailed in Table IV.

TABLE IV. Fuzzy Rules of the 'Congestion' Node with its Parent Nodes

| Rule number | Signage | Weather conditions | Occurrence of events | Congestion |
| :---: | :---: | :---: | :---: | :---: |
| 1 | Bad | extremes | High | high |
| 2 | Bad | extremes | Medium | high |
| 3 | Bad | extremes | Low | medium |
| 4 | Bad | medium | High | high |
| 5 | Bad | medium | Medium | medium |
| 6 | Bad | medium | Low | medium |
| 7 | Bad | normal | High | medium |
| 8 | Bad | normal | Medium | medium |
| 9 | Bad | normal | Low | low |
| 10 | Medium | extremes | High | high |
| 11 | Medium | extremes | Medium | medium |
| 12 | Medium | extremes | Low | medium |
| 13 | Medium | medium | High | medium |
| 14 | Medium | medium | Medium | medium |
| 15 | Medium | medium | Low | medium |
| 16 | Medium | normal | High | medium |
| 17 | Medium | normal | Medium | medium |
| 18 | Medium | normal | Low | low |
| 19 | Good | extremes | High | high |
| 20 | Good | extremes | Medium | medium |
| 21 | Good | extremes | Low | medium |
| 22 | Good | medium | High | medium |
| 23 | Good | medium | Medium | medium |
| 24 | Good | medium | Low | low |
| 25 | Good | normal | Low | medium |
| 26 | Good | normal | Medium | low |
| 27 | Good | normal | Low | low |

The inference mechanism is triggered by initializing the input variables with precise values representing the peak of the Gaussian distribution and activating a set of fuzzy rules. This mechanism uses the Sugeno inference system. The aim is to identify degrees of membership to each fuzzy subset. The calibration of these degrees provides the CPTs of the BN.

Consider the example of inferring the congestion node knowing that the signage is average, the methodological conditions are normal, and the occurrence of traffic blocking/interfering events is low. The initial values of the input variables represented in rule 18 of Table VI will feed the fuzzy inference system. The latter is implemented with the Fispro software.

The results of the fuzzy inference are illustrated in Fig. 4, thereafter; the different results are aggregated, in order to combine them into a single value for each state. This value is the result of the union of the different conclusions of the rules activated with the max method.



Fig. 4. Fuzzy Inference of the Variable 'Congestion.
The conclusions of the activated rules of rule 18 are summarized in Table V. Thus, the low value of congestion is 0.98 , and the average value is 0.020 . Now, since each possibility of a fuzzy subset must be greater than zero, a value
of 0.001 is given to the null probability, in this case the high value is 0.001 .

Congestion (low) $=\max (0.98,0.015,0.008)=0.98$.
Congestion (medium) $=\max (0.015,0.008,0.020)=0.020$.
Congestion (high) $=0.001$.
The conditional probabilities for the different states of the variable 'congestion' of the rule 18 is calculated in the following way:
$\mathrm{P}($ Congestion $=$ low $\mid$ Occurrence events $=$ low, Weather $=$ normal and Signage $=$ medium) $=$ $0.98 /(0.98+0.020+0.001)=0.979$.

P (Congestion = medium | Occurrence of events = low, Weather $=$ normal and Signage $=$ medium) $=$ $0.020 /(0.98+0.020+0.001)=0.019$.

P (Congestion $=$ high | Occurrence of events = low, Weather $=$ normal and Signage $=$ medium) $=$ $0.001 /(0.98+0.020+0.001)=0.001$.

TABLE V. Degree of Membership for each Fuzzy Subset of the Variable 'Congestion

| Rule activated | Language value of the output <br> variable | Degree of <br> membership |
| :--- | :--- | :--- |
| R27 | Low | 0.015 |
| R26 | Low | 0.015 |
| R24 | Low | 0.015 |
| R23 | Medium | 0.015 |
| R18 | Low | 0.98 |
| R17 | Medium | 0.020 |
| R15 | Medium | 0.020 |
| R14 | medium | 0.020 |
| R9 | Low | 0.008 |
| R8 | medium | 0.008 |
| R6 | medium | 0.008 |

## C. Anticipation of Scenarios and Interpretation of Results

After constructing the Bayesian network using Open Markov tool, it is used to deduce the probabilities of certain events by setting evidences (states) for certain nodes and study their effects through the propagation of their probabilities on the child nodes. At this level, the input parameters' impact on the occurrence of delay is studied through four scenarios listed as follows:

- Scenario 1: favorable road environment and delivery areas input parameters, unfavorable transport company input parameters.
- Scenario 2: unfavorable road environment and delivery areas input parameters, favorable transport company input parameters.
- Scenario 3: favorable road environment and delivery areas input parameters, favorable transport company input parameters.
- Scenario 4: unfavorable road environment and delivery areas input parameters, unfavorable transport company input parameters.
The input parameters related to the transport company correspond to those related to the vehicles, the staff (drivers, planners ...) and the planning systems.

The input parameters related to the road environment and delivery areas correspond to those related to the road, traffic and warehouses.

The four scenarios corresponding to different configurations of the input node states are detailed in Table VII.

After feeding the BN with the states of each scenario, the inference mechanism provides probability propagation over intermediate effects and final impacts to quantify delay occurrence. Table VIII, shows the probability distribution for some nodes in the network.

TABLE VI. Conditional Probability Table of the 'Congestion' Node

|  |  |  |  |  | Conditional probability |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Rule number | Signage | Weather conditions | Occurrences of events | Congestion | Low | medium | high |
| 1 | bad 0.22 | extremes 0.18 | high 0.21 | high | 0.001 | 0.015 | 0.984 |
| 2 | bad 0.22 | extremes 0.18 | medium 0.52 | high | 0.001 | 0.020 | 0.979 |
| 3 | bad 0.22 | extremes 0.18 | low 0.78 | medium | 0.001 | 0.979 | 0.020 |
| 4 | bad 0.22 | medium 0.5 | high 0.21 | high | 0.001 | 0.020 | 0.979 |
| 5 | bad 0.22 | medium 0.5 | medium 0.52 | medium | 0.001 | 0.988 | 0.011 |
| $\ldots$ | $\cdots$ | $\cdots$ | $\cdots$ | $\ldots$ | ... | ... | ... |
| 18 | medium 0.51 | normal 0.78 | low 0.78 | low | 0.979 | 0.020 | 0.001 |
| 19 | good 0.81 | extremes 0.18 | high 0.21 | high | 0.001 | 0.015 | 0.984 |
| 20 | good 0.81 | extremes 0.18 | medium 0.52 | medium | 0.006 | 0.988 | 0.006 |
| $\cdots$ | $\cdots$ | $\cdots$ | $\cdots$ | $\cdots$ | $\ldots$ | $\ldots$ | $\ldots$ |
| 25 | good 0.81 | normal 0.78 | high 0.21 | medium | 0.015 | 0.984 | 0.001 |
| 26 | good 0.81 | normal 0.78 | medium 0.52 | low | 0.979 | 0.020 | 0.001 |
| 27 | good 0.81 | normal 0.78 | low 0.78 | low | 0.979 | 0.020 | 0.001 |

TABLE VII. Description of the Scenarios According to the Values of the Input Parameters

| Input parameter | Value |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Scenario 1 | Scenario 2 | Scenario 3 | Scenario 4 |
| Road environment and delivery areas parameters |  |  |  |  |
| Road design | good | bad | good | bad |
| Lighting | good | bad | good | bad |
| Post-accident road cleaning | appropriate | inappropriate | appropriate | inappropriate |
| Signage | good | bad | good | bad |
| Weather conditions | normal | extremes | normal | extreme |
| Occurrence of events that block/impede traffic | low | high | low | high |
| Availability of delivery bays | high | low | high | low |
| Resources Availability | high | low | high | low |
| Occurrence of internal events | low | high | low | high |
| Scheduling of arrival times | good | bad | good | bad |
| Transport company parameters |  |  |  |  |
| Driving style | bad | good | good | bad |
| Driver condition | bad | good | good | bad |
| Driver behavior | bad | good | good | bad |
| Vehicle condition | bad | good | good | bad |
| Resource allocation | bad | good | good | bad |
| Estimated departure time | bad | good | good | bad |
| Number of exchanges | high | Low | low | high |

TABLE VIII. Probability Distribution for Bayesian Network Nodes

| Node | State | Scenario 1 | Scenario $2$ | Scenario <br> 3 | Scenario <br> 4 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Congestion | Low | 0.9790 | 0.0010 | 0.9790 | 0.0010 |
|  | Medium | 0.0020 | 0.0150 | 0.0020 | 0.0150 |
|  | High | 0.0010 | 0.9840 | 0.0010 | 0.9840 |
| Occurrence of a breakdown | high | 0.9790 | 0.0010 | 0.0010 | 0.9790 |
|  | Medium | 0.0200 | 0.0020 | 0.0020 | 0.0174 |
|  | Low | 0.0027 | 0.9790 | 0.9790 | 0.0010 |
| Occurrence of an accident | Low | 0.0022 | 0.0012 | 0.9574 | 0.0010 |
|  | Medium | 0.0418 | 0.9574 | 0.0416 | 0.0173 |
|  | high | 0.9559 | 0.0214 | 0.0010 | 0.9817 |
|  | Low | 0.0209 | 0.9166 | 0.9166 | 0.0052 |
| Occurrence of ticket | Medium | 0.0052 | 0.0592 | 0,0592 | 0.0209 |
|  | high | 0.9738 | 0.0242 | 0.0242 | 0.9738 |
| Accessibili ty to destination points | High | 0.9635 | 0.0010 | 0.9635 | 0.0010 |
|  | Medium | 0.0355 | 0.0155 | 0.0355 | 0.0155 |
|  | Low | 0.0010 | 0.9835 | 0.0010 | 0.9835 |
| Delay | Low | 0.0017 | 0.0050 | 0.9718 | 0.0010 |
|  | Medium | 0.0861 | 0.9624 | 0.0272 | 0.0160 |
|  | High | 0.9121 | 0.0327 | 0.0010 | 0.9830 |

In the case of the first scenario, the occurrence of congestion is low with a probability of $97.9 \%$. Concerning the occurrence of a breakdown and ticket, and accident are important with respectively $97.9 \%$ and $97.3 \%$ and $95.5 \%$. As for the accessibility to the destination, point tends to be high with $96.3 \%$. Therefore, the probability of the occurrence of delay is important with a value of $91.1 \%$.

For the second scenario, the probability of congestion occurrence is high with a probability of $98.4 \%$. Regarding the occurrence of accident is more likely to be 'medium' with a probability of $95.7 \%$, as for the occurrence of breakdown and ticket are low with respectively $97.9 \%$ and $91.6 \%$, In addition, the accessibility to the destination point tends to be low with $98.3 \%$ which leads to an average risk of occurrence of delay of 96.2\%

For the third scenario, the inference model predicts a low probability of congestion occurrence with a rate of $97.9 \%$. Also, the risks related to the occurrence of an accident, breakdown and a ticket are low with respectively $95.7 \%$, $97.9 \%$ and $91.6 \%$. In addition, the accessibility to the destination point tends to be high with $96.3 \%$. Therefore, the probability of delay occurrence is very low with $97.1 \%$.

For the fourth scenario, congestion tends to be high with a rate of $98.4 \%$. Also, the risks of the occurrence of an accident, a breakdown or a ticket are high with respectively $98.1 \%$, $97.9 \%$ and $97.3 \%$. As for the accessibility to the destination, point is low with a percentage of $98.3 \%$. Hence the highest probability of the occurrence of delay with $98.3 \%$.

Based on the results of the inference of the first two scenarios, we can conclude that the parameters related to the transport company have more impact on the occurrence of delivery delay than those related to road and delivery environment.

## D. Sensitivity Analysis

The sensitivity analysis identifies the factors ranked according to those that have more impact on the probability of a node [65]. The Fig. 5 shows the tornado diagram [66] of the "delay occurrence" sensitivity analysis. According to the figure, variables such as vehicle condition, resources availability, estimated departure time, number of exchanges, and resource allocation contribute more to the occurrence of late deliveries. Poor vehicle condition is the main parameter influencing the risk of delay. This can be justified by its resulting events such as the occurrence of breakdowns and accidents, as these have a significant impact on the occurrence of such risk.

## E. Partial Validation

In order to validate the proposed model, the paper uses partial validation allowing the verification of three axioms presented by [67] and opted by various researchers such as [68], [69]: (1) The occurrence of change (increase/decrease) in the probability of the parent node thus changes the probability of the child node; (2) The values of the child nodes must be consistently affected by the changes made to the probability distributions relative to the parent node; In the case of a node with more than one parent (e.g., $x$ and $y$ ), the overall effect of $x$ and $y$ must be greater than the individual effects of parent $x$ or parent y.

For example, when the probability of "road design = good" increases from $70 \%$ to $75 \%$, the probability of "road infrastructure condition $=$ good" and "road environment $=$ good" increases from $77 \%$ to $80 \%$ and $84 \%$ to $86 \%$ respectively. In light of this variation, when the probability of "Occurrence of events that block/slow traffic=low" increases from $74 \%$ to $78 \%$, the probability of "congestion=low" and "road environment=good" increases from $78 \%$ to $82 \%$ and $87 \%$ to $90 \%$ respectively, which is consistent with the axiom. Similarly for the other nodes of the graph.

Sensitivity for Occurrence_of_delay=high
Current value: 0.177267 Reachable range: [ 0.167972 .. 0.189252$]$


Fig. 5. Sensitivity Analysis for Occurnce of Delay.

## IV. DISCUSSION

In this paper, an analysis of potential delivery delays is developed using a Bayesian fuzzy model. BNs have been used in various existing studies to analyze the risk of delay in different areas such as maritime transport[45], [70], rail transport [71] and air transport [72]. Compared to the existing works, the developed model focuses on the occurrence of delay in the road freight transport domain. This model consists of many internal and external factors that cause delay to occur. Sensitivity analysis and interpretation of the results of four scenarios show that the internal factors related to the transport companies have a stronger effect on the occurrence of late deliveries than the external factors. This means that the transport company decisions in terms of resource selection, in addition to planning relevance, have a considerable effect on delivery reliability than road and delivery events such as congestion, weather conditions and availability of delivery bays. Therefore, optimized resource (physical and material) allocation to the right routes and a smart routing planning design plays an important role in ensuring on-time deliveries. In order to validate the results of this model, an example test of three axioms is performed.

## V. CONCLUSION

The respect of delivery deadlines is crucial to ensure the quality of logistics services. Unfortunately, it often happens that this deadline is not respected, leading to a series of more or less unfortunate consequences. This article focuses on predicting the risks of delays in deliveries with the aim of anticipating them in order to either avoid them or be better prepared to deal with them and reduce the impact of poor quality of service. To do this, the article proposes a fuzzy Bayesian model combining the Bayesian approach and fuzzy logic in order to monitor the occurrence of delivery delays. This model is based on a set of factors causing the delay of deliveries and their causal relationships represented by a causal graph. Fuzzy logic intervenes by the generation of fuzzy rules based on conditional probability tables. Such a model is particularly effective, especially for the type of problem dealt with through this article. It is positioned as an excellent alternative to deep learning for making predictions in the absence of massive data.

One of the limitations of the proposed model is the identification of all the factors that cause delivery delays, the lack of integration of all these factors can affect the effectiveness of this model in correctly predicting possible delays.

The generalization of the model to all risks that can degrade the quality of delivery services such as damage, theft and loss, is a potential perspective to the work presented here. Similarly, a comparative study between a Bayesian-fuzzy model and a model derived from deep-learning around the prediction of delivery risks and the management of the crises that follow are very promising avenues of research.

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